



# ANARRES\_t: A SAM Based Global CGE Model

Scott McDonald

Addresses for correspondence:

Scott McDonald,  
cgemod  
Email: [scott@cgemod.org.uk](mailto:scott@cgemod.org.uk)

## Abstract

This paper provides a technical description of a global computable general equilibrium (CGE) model that is calibrated from a Social Accounting Matrix (SAM) representation of the Global Trade Analysis Project (GTAP) database. Two distinctive features of the model is the treatment of nominal and real exchange rates and the use of a ‘dummy’ region, known as ‘globe’, that allows for the recording of inter-regional transactions where either the source or destination is not identified.

*Keywords:* Computable General Equilibrium; GTAP.

*JEL classification:* D58; R13; F49.

**THIS DOCUMENT IS A FAITHFUL TECHNICAL REPORT OF THE ANARRES\_t  
MODEL. HOWEVER, READERS SHOULD BE AWARE THAT THE ONLY  
DOCUMENTATION THAT IS GUARANTEED EXACT IS THE MODEL CODE.**



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## 1. Introduction

This paper provides a technical description of a variant of a Social Accounting Matrix (SAM) based Global Computable General Equilibrium (CGE) model that has been calibrated using data derived from the Global Trade Analysis Project's (GTAP) database. The model is a member of a family of CGE models that model trade relationships using principles described in the 1-2-3 model (de Melo and Robinson, 1989; Devarajan, *et al.*, 1990). More specifically this model is a direct descendant of an early US Department of Agriculture model (see Robinson *et al.*, 1990; Kilkenny, 1991) and NAFTA (see Robinson *et al.*, 1993). However numerous features of this model stem from other developments in CGE modelling over the last 25 years; some of these sources of inspiration are direct and easily identified, e.g., analysis used in the World Development Report, 1995 (Lewis, Robinson, and Wang), the IFPRI standard model (Lofgren *et al.*, 2002) and the PROVIDE Project model (McDonald, 2003), others are indirect and easily identified, e.g., the GTAP model (Hertel, 1997), while others are both direct and indirect but less easily identified; a substantial debt is owed to the community of CGE modellers. In addition, the model owes a lot to the development of the SAM approach to national accounting, e.g., Stone (1962a and b) and Pyatt (1991), and the SAM approach to modelling, e.g., Pyatt (1987), Drud *et al.*, (1986).

The underlying approach to multi-region modelling for this CGE model is the construction of a series of single country CGE models that are linked through their trading relationships.<sup>1</sup> As is common with all known CGE models the price systems in the model are linear homogenous and hence the focus is upon movements in relative, rather than absolute, prices. Consequently, each region in the model has its own numéraire price, typically the consumer price index (CPI), and a nominal exchange rate, while the model as a whole requires a numéraire, which is an exchange rate index for a number of reference regions. As such this model contains a fundamentally different philosophical approach to global modelling to that found in the GTAP model.<sup>2</sup> Behind this difference lies a deep theoretical

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<sup>1</sup> As far as is known this approach is used in all global CGE models, including those used to analyse climate change.

<sup>2</sup> While the GTAP model, and others derived from the GTAP model, do not explicitly contain nominal exchange rates they are implicit and are fixed. Thus, while these models assert the existence of a single global numéraire, they do in fact have  $(r + 1)$  numéraire where  $r$  is the number of regions in the model and for which the, implicit, exchange rate is fixed and serves as the region specific numéraire.

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debate about how comparative static and finite horizon dynamic CGE models should value transfers associated with the capital account of the balance of payments (see Robinson, 2004).

A distinctive feature of the model is the use of a ‘dummy’ region, known as Globe, that allows for the recording of inter-regional transactions where either the source or destination are not identified. Examples of such transactions include trade and transportation margins and data on remittances. The Globe construct provides a general method for dealing with any transactions data where full bilateral information is missing.

The rest of this paper is organised as follows. Section 2 reviews the data used in the model; this section also provides a brief description of how the data were transformed from the GTAP database into a SAM. This is followed in section 3 by a descriptive overview of the model and then, in section 4, by a formal description of the model’s equations. The description in section 4 is based upon a default setting for the model closure rules; one of the model’s key features is the flexibility of the closure rules and consequently section 5 considers the alternatives built into the model’s basic structure. All global CGE models are large and therefore present a series of potential implementation problems; section 6 briefly reviews some of the programmes that have been developed to support the basic model and provides some guidelines for use of this class of model.

## 2. Model Data

The data used in the model were derived from the GTAP database (see Hertel, 1997) using a three-dimensional Social Accounting Matrix (SAM) method for organising the data. Details of the method used to generate a SAM representation are reported in McDonald and Thierfelder (2019)<sup>3</sup> while a variety of reduced form representations of the SAM and methods for augmenting the GTAP database are reported in McDonald and Thierfelder (2004b) and McDonald and Sonmez (2004) respectively. Detailed descriptions of the data are provided elsewhere so the discussion here is limited to the general principles.

### 2.1 Global Social Accounting Matrix

The Global SAM can be conceived of as a series of single region SAMs that are linked through the trade accounts; it is particularly valid in the context of the GTAP database to note that the ONLY way in which the regions are linked directly in the database is through commodity trade transactions although there are some indirect links through the demand and supply of trade and transport services. Specifically, the value of exports, valued free on board (*fob*) from source  $x$  to destination  $y$  must be exactly equal to the value of imports valued *fob* to destination  $y$  from source  $x$ , and since this holds for all commodity trade transactions the sum of the differences in the values of imports and exports by each region must equal zero. However, the resultant trade balances do not fully accord with national accounting conventions because other inter regional transactions are not recorded in the database (see McDonald and Sonmez, 2004). A description of the transactions recorded in a representative SAM for a typical region in the database is provided in Table 1.

A SAM is a transactions matrix; hence each cell in a SAM simply records the value of the transactions between the two agents identified by the row and column accounts. The selling agents are identified by the rows, i.e., the row entries record the incomes received by the identified agent, while the purchasing agents are identified by the columns, i.e., the column entries record the expenditures made by agents. As such a SAM is a relatively compact form of double entry bookkeeping that is complete and consistent and can be used to present the National Accounts of a country in a single two-dimensional matrix (see UN, 1993,

<sup>3</sup> This is revised and updated version of GTAP Technical Paper 13 (McDonald and Thierfelder (2004a)) that defined how GTAP data could be rendered in SAM format.

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for a detailed explanation of the relationship between conventional and SAM presentations of National Accounts). A SAM is complete in the sense that the SAM should record ALL the transactions within the production boundary of the National Accounts, and consistent in the sense that income transactions by every agent are exactly matched by expenditure transactions of other agents. A fundamental consequence of these conditions is that the row and column totals of the SAM for each region must be identical, and hence the SAM provides a complete characterisation of current account transactions of an economy as a circular (flow) system. In the context of a global SAM the complete and consistent conditions need extending to encompass transactions between regions; this simply requires that each and every import transaction by a region must have an identical counterpart export transaction by another region. This is enough to ensure that the resultant global SAM provides a characterisation of current account transactions of the global economy as a circular (flow) system.

Given these definitions of a SAM the transactions recorded in a SAM are easily interpreted. In Table 1 the row entries for the commodity accounts are the values of commodity sales to the agents identified in the columns, i.e., intermediate inputs are purchased by activities (industries etc.), final consumption is provided by households, the government and investment demand and export demand is provided by the all the other regions in the global SAM and the export of margin services. The commodity column entries deal with the supply side, i.e., they identify the accounts from which commodities are purchased so to satisfy demand. Specifically, commodities can be purchased from either domestic activities – the domestic supply matrix valued inclusive of domestic trade and transport margins – or they can be imported – valued exclusive of international trade and transport margins. In addition to payments to the producing agents – domestic or foreign – the commodity accounts need to make expenditures with respect to the trade and transport services needed to import the commodities and any commodity specific taxes.



**Table 1 Social Accounting Matrix for a Region in the Global Social Accounting Matrix**

	<b>Commodities</b>	<b>Activities</b>	<b>Factors</b>	<b>Households</b>	<b>Government</b>	<b>Capital</b>	<b>Margins</b>	<b>Rest of World</b>	<b>Totals</b>
<b>Commodities</b>	0	Combined Intermediate Use Matrix	0	Private Consumption	Government Consumption	Investment Consumption	Exports of Margins (fob)	Exports of Commodities (fob)	Total Demand for Commodities
<b>Activities</b>	Domestic Supply Matrix	0	0	0	0	0	0	0	Total Domestic Supply by Activity
<b>Factors</b>	0	Expenditure on Primary Inputs	0	0	0	0	0	0	Total Factor Income
<b>Households</b>	0	0	Distribution of Factor Incomes	0	0	0	0	0	Total Household Income
<b>Government</b>	Taxes on Commodities	Taxes on Production Taxes on Factor Use	Direct/Income Taxes	Direct/Income Taxes	0	0	0	0	Total Government Income
<b>Capital</b>	0	0	Depreciation Allowances	Household Savings	Government Savings	0	Balance on Margins Trade	Foreign Savings	Total Savings
<b>Margins</b>	Imports of Trade and Transport Margins	0	0	0	0	0	0	0	Total Income from Margin Imports
<b>Rest of World</b>	Imports of Commodities (fob)	0	0	0	0	0	0	0	Total Income from Imports
<b>Totals</b>	Total Supply of Commodities	Total Expenditure on Inputs by Activities	Total Factor Expenditure	Total Household Expenditure	Total Government Expenditure	Total Investment	Total Expenditure on Margin Exports	Total Expenditure on Exports	

The GTAP database provides complete coverage of bi lateral transactions in commodities – these are valued free on board (*fob*) - but only provides partial coverage of transactions in trade and transport margins. Specifically, the imports of trade and transport margins by each region are directly associated with the imports of specific commodities, hence for each commodity import valued *fob* the source and destination regions are identified and the value of each trade and transport margin service used is identified. The sum of the values of trade and transport services and the *fob* value of the commodity imports represent the carriage insurance and freight (*cif*) paid value of each imported commodity. But the source regions of the trade and transport services are NOT identified, and similarly the values of exports of trade and transport services by a region do NOT identify the destination regions. To overcome this lack of information an artificial region called Globe is included in the database. This region collects together all the exports of trade and transport services by other regions as its imports and then exports these to other regions to satisfy their demand for the use of trade and transport services associated with commodity imports. By construction the value of imports by Globe for every trade and transport margin service must exactly equal the value of exports for the corresponding trade and transport service. However, this does not mean that the trade balance between Globe and each and every region must exactly balance, rather it requires that the sum of Globe's trade balances with other regions is exactly equal to zero.

An important feature of the construction of a SAM can be deduced from the nature of the entries in the commodity account columns. By definition the column and row totals must equate and these transaction totals can be expressed as an implicit price times a quantity, and the quantity of a commodity supplied must be identical to the quantity of a commodity demanded. The column entries represent the expenditures incurred in order to supply a commodity to the economy and hence the implicit price must be exactly equal to the average cost incurred to supply a commodity. Moreover, since the row and column totals equate and the quantity represented by each corresponding entry must be same for the row and column total the implicit price for the row total must be identical to average cost incurred to supply the commodity. Hence the column entries identify the components that enter into the formation of the implicit prices in the rows, and therefore identify the price formation process

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for each price in the system. Typically, a SAM is defined such that the commodities in the rows are homogenous and that all agents purchase a commodity at the same price.

Total income to the activity accounts is identified by the row entries. In the simple representation of production in the GTAP database each activity makes a single commodity and each commodity is made by a single activity, which means that the domestic supply matrix is a diagonal (square) matrix. The expenditures on inputs used in production are recorded in the activity columns. Activities use intermediate inputs, which in this version of the database are record as composites of domestically produced and imported commodities, primary inputs and pay taxes on production and factor use. For each region the sum of the payments to primary inputs and on production and factor use taxes by activity is equal to the activity's contribution to the value added definition of GDP while the sum over activities equals the region's value added measure of GDP.

The remaining accounts relate to the institutions in the SAM. All factor incomes are distributed to the single private household after making allowance for depreciation of physical capital and the payment of direct (income) taxes on factor incomes. Incomes from factor sales are also the sole source of income to the household account. Three categories of expenditures by the household account are recorded; direct (income) taxes, savings and consumption. The government receives incomes from commodity taxes, production taxes and direct taxes on factor and household incomes, and uses that income to pay for consumption and for savings. In the basic form of the database government savings are set to zero for all regions; this stems from the reduced form representation of intra institutional transactions provided by the GTAP database (see McDonald and Thierfelder, 2004b).<sup>4</sup> There are therefore five sources of savings in each region: depreciation, household/private savings, government savings, balances on trade in margin services and balances on trade in commodities, but only a single expenditure activity – investment (commodity) demand.

As should be apparent from the description of the SAM for a representative region the database is strong on inter regional transactions but relatively parsimonious on intra-regional transactions.

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<sup>4</sup> McDonald and Sonmez (2004) demonstrate that it is straightforward to overcome this limitation of the database. The model described in this paper operates whether the government savings are zero or non-zero.

## 2.2 Other GTAP Data

In addition to the transactions data the GTAP database contains other data that can be used with this model, and/or variants of the model. The most obviously useful data are the import and primary factor elasticity data used in the GTAP model; the programme used to derive an aggregation of the SAM also contains a routine for aggregating these elasticities for use in this model. However, the GTAP elasticities are only a subset of the elasticities used in this model and it is therefore necessary to provide other elasticities even when using the GTAP elasticity data.

Other data of interest to modellers include estimates of energy usage and emissions and land use (carbon sinks). None of these data are used in this variant of the model.

## 2.3 Database Dimensions

The dimensions of the SAM are determined by the numbers of accounts within each aggregate group identified in Table 1, while the actual numbers of accounts in each group of accounts are defined for version 5.4 and 6.0 of the GTAP database in Table 2. Given the large number of accounts in the SAMs for each region and the relatively large number of regions the total number of cells in the global SAM is very large, although only slightly over 10 percent of the cells actually contain non zero entries; nevertheless this still means that the GTAP database contains some 4 million transaction values, which implies that there are some 8 million possible prices and quantities that can be deduced from the database. Even allowing for the implications of adopting the law of one price for transactions in the rows of each region’s SAM and for other ways of reducing the numbers of independent prices and quantities that need to be estimated in a modelling environment, it is clear that the use of the GTAP database without aggregation is likely to generate extremely large models (in terms of the number of equations/variables). Consequently, except in exceptional circumstances all CGE models that use the GTAP data operate with aggregations of the database.

**Table 2 Dimensions of the Global Social Accounting Matrix**

Account Groups	Sets	Total Number of Accounts			
		GTAP 5.4	GTAP 6.0	GTAP 7.1	GTAP 8a

<b>Commodities</b>	<b>C</b>	<b>57</b>	<b>57</b>	<b>57</b>	<b>57</b>
<b>Activities</b>	<b>A</b>	<b>57</b>	<b>57</b>	<b>57</b>	<b>57</b>
<b>Factors</b>	<b>F</b>	<b>5</b>	<b>5</b>	<b>5</b>	<b>5</b>
<b>Taxes</b>	$(2*r)+(1*f)$ <b>+3</b>	<b>164</b>	<b>182</b>	<b>232</b>	<b>395</b>
<b>Other Domestic Institutions</b>	<b>3</b>	<b>3</b>	<b>3</b>	<b>3</b>	<b>3</b>
<b>Margins</b>	$3*r$	<b>234</b>	<b>261</b>	<b>336</b>	<b>387</b>
<b>Trade</b>	<b>R</b>	<b>78</b>	<b>87</b>	<b>112</b>	<b>129</b>
<b>Total</b>		<b>598</b>	<b>652</b>	<b>802</b>	<b>1,033</b>
<b>Total Number of Cells in the Global SAM</b>		<b>27,893,112</b>	<b>36,984,048</b>	<b>72,038,848</b>	<b>137,654,481</b>

## Overview of the Model

### 3.1 Behavioural Relationships

The within regional behavioural relationships are standard in this variant of the model; they are similar to those in smod\_t and it is easy to make them more elaborate, but the focus of this variant is international trade relationships. The activities are assumed to maximise profits using technology characterised by Constant Elasticity of Substitution (CES) and/or Leontief production functions between aggregate primary inputs and aggregate intermediate inputs, with a two-level nest of CES production functions over primary inputs and Leontief technology across intermediate inputs. The household maximises utility subject to preferences represented by a Stone-Geary utility function, i.e., a linear expenditure system, having first paid income taxes and having saved a fixed or flexible proportion of after tax income.<sup>5</sup>

The Armington ‘insight’ is used for trade. Domestic output is distributed between the domestic market and exports according to a two-stage Constant Elasticity of Transformation (CET) function. In the first stage a domestic producer allocates output to the domestic or export market according to the relative prices for the commodity on the domestic market and the composite export commodity, where the composite export commodity is a CET aggregate of the exports to different regions – the distribution of the exports between regions being determined by the relative export prices to those regions. Consequently, domestic producers are responsive to prices in the different markets – the domestic market and all other regions in the model – and adjust their volumes of sales according relative prices. The elasticities of transformation are commodity and region specific. The CET functions across exports can be switched off so that export supplies are determined by import demands.<sup>6</sup>

Domestic demand is satisfied by composite commodities that are formed from domestic production sold domestically and composite imports. This process is modelled by three-levels of CES functions. At the bottom level a composite import commodity is a CES aggregate of imports from different regions with the quantities imported from different regions being responsive to relative prices and another composite import commodity is a Leontief aggregate of imports from different regions with the quantities being fixed proportions of the volume of

<sup>5</sup> With appropriate parameter specification the LES collapses to a Cobb-Douglas specification.

<sup>6</sup> Switching off the CET function allows the model to function in a similar manner to the GTAP model.

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import demand. This second composite commodity is introduced for the treatment of imports whose volumes are small and can, as a consequence have large terms of trade effects. The second level is a Leontief aggregate of the two composite commodities formed at the bottom level, which defines the volumes of composite imports. The top level defines a composite consumption commodity as a CES aggregate of a domestic commodity and a composite import commodity with the mix being determined by the relative prices. The elasticities of substitution are commodity and region specific.<sup>7</sup> Hence the optimal ratios of imports to domestic commodities and exports to domestic commodities are determined by first order conditions based on relative prices. The price and quantity systems are described in greater detail below

Most commodity and activity taxes are expressed as *ad valorem* tax rates, while income taxes are defined as fixed proportions of household incomes. Import duties and export taxes apply to imports and exports, while sales taxes are applied to all domestic absorption, i.e., imports are subject to sequential import duties and sales taxes, and VAT is applied to household demand. Production taxes are levied on the value of output by each activity, while activities also pay taxes on the use of specific factors. Factor income taxes are charged on factor incomes after allowance for depreciation after which the residual income is distributed to households. Income taxes are taken out of household income and then the households are assumed to save a proportion of disposable income. This proportion is either fixed or variable according to the closure rule chosen for the capital account.

Government expenditure consists of commodity (final) demand, which is assumed to be in fixed proportions in real/volume terms. Hence government saving, or the internal balance, is defined as a residual. However, the closure rules for the government account allow for various permutations. In the base case it is assumed that the tax rates and volume of government demand are fixed and government savings are calculated as a residual. However, the tax rates can all be adjusted using various forms of scaling factors; hence for instance the value of government savings can be fixed and one of the tax scalars can be made variable thereby producing an estimate of the constrained optimal tax rate. If the analyst wishes to change the relative tax rates across commodities (for import duties, export taxes and sales taxes) or across activities (for production taxes) then the respective tax rate parameters can be

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<sup>7</sup> This is different to the GTAP model where the elasticities are only commodity specific.

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altered via a second adjuster. Equally the volume of government consumption can be changed by adjusting the closure rule with respect the scaling adjuster attached to the volumes of government consumption. The patterns of government expenditure are altered by changing the parameters that control the pattern of government expenditure (*qgdconst*).

Total savings come from the households, the internal balance on the government account and the external balance on the trade account. The external balance is defined as the difference between the value of total exports and total imports, converted into domestic currency units using the exchange rate. In the base model it is assumed that the exchange rates are flexible and hence that the external balances are fixed. Alternatively, the exchange rates can be fixed and the external balances can be allowed to vary. Expenditures by the capital account consist solely of commodity demand for investment. In the base solution it is assumed that the shares of investment in total domestic final demand are fixed and that household savings rates adjust so that total expenditures on investment are equal to total savings, i.e., the closure rule presumes that savings are determined by the level of investment expenditures. The patterns of investment volume are fixed, and hence the volume of each commodity changes equiproportionately according to the total values of domestic final demand. It is possible to fix the volumes of real investment and then allow the savings rates, by households, to vary to maintain balances in the capital account, and it is possible to change the patterns of investment by changing the investment parameters (*qinvdconst*).



**Table 3 Behavioural Relationships for a Global CGE Model**

	<b>Commodities</b>	<b>Activities</b>	<b>Factors</b>	<b>Households</b>	<b>Government</b>	<b>Investment</b>	<b>Margins</b>	<b>Rest of World</b>	<b>Prices</b>
<b>Commodities</b>	0	Leontief Input-Output Coefficients	0	Stone-Geary Utility Functions	Fixed Exogenously	Fixed Shares of Savings	Three-Stage CET Functions	Three-Stage CET Functions	Consumer Commodity Price
<b>Activities</b>	Total Supply from Domestic Production	0	0	0	0	0	0	0	Activity Prices
<b>Factors</b>	0	Two-stage CES Production Functions	0	0	0	0	0	0	Factor Prices
<b>Households</b>	0	0	Fixed Shares of Factor Income	0	0	0	0	0	
<b>Government</b>	<i>Ad valorem</i> tax rates Specific Tax rates	<i>Ad valorem</i> tax rates on Output and Factor Use	Average tax rates	Average tax rates	0	0	0	0	
<b>Savings</b>	0	0	Shares of Factor Incomes	Shares of household income	Government Savings (Residual)	0	Current Account 'Deficit' on Margins Trade	Current Account 'Deficit'	
<b>Margins</b>	Fixed Technical Coefficients	0	0	0	0	0	0	0	
<b>Rest of World</b>	Three-Stage CES Functions	0	0	0	0	0	0	0	
<b>Prices</b>	Producer Prices Domestic and World Prices for Imports	Value Added Prices							

**Table 4 Transactions Relationships for a for a Global CGE Model**

	<b>Commodities</b>	<b>Activities</b>	<b>Factors</b>	<b>Households</b>
<b>Commodities</b>	0	$(PQD_c * QINTD_c)$	0	$(PQCD_c * QCD_c)$
<b>Activities</b>	$(PDS_c * QDS_c)$	0	0	0
<b>Factors</b>	0	$(WFA_{f,a} * FD_{f,a})$	0	0
<b>Households</b>	0	0	$\sum_f \left( \begin{matrix} hvas_{h,f} \\ *YF_f \end{matrix} \right)$	0
<b>Government</b>	$\left( \begin{matrix} TM_{w,c} * PWM_{w,c} \\ *QMR_{w,c} * ER \end{matrix} \right)$ $\left( \begin{matrix} TE_{w,c} * PWE_{w,c} \\ *QER_{w,c} * ER \end{matrix} \right)$ $(TS_c * PQS_c * QQ_c)$ $(TV_c * PQD_c * QQ_c)$	$(TX_a * PX_a * QX_a)$ $\left( \begin{matrix} TF_{f,a,r} * WF_{f,r} \\ *WFDIST_{f,a,r} * FD_{f,a,r} \end{matrix} \right)$	$\left( \begin{matrix} TYF_{f,r} * \left( \begin{matrix} YF_{f,r} - \\ \left( \begin{matrix} deprec_{f,r} \\ *YF_{f,r} \end{matrix} \right) \end{matrix} \right) \end{matrix} \right)$	$(TYH_h * YH_h)$
<b>Savings</b>	0	0	$(deprec_{f,r} * YF_{f,r})$	$\left( \begin{matrix} YH_{h,r} \\ *(1 - TYH_{h,r}) \end{matrix} \right) * (SHH_{h,r})$
<b>Margins</b>	$(PT_c * QT_{w,c})$	0	0	0
<b>Rest of World</b>	$\left( \begin{matrix} PWMFOB_{w,c} \\ *QMR_{w,c} * ER \end{matrix} \right)$	0	0	0
<b>Total</b>	$(PQD_c * QQ_c)$	$(PX_a * QX_a)$	$YF_f$	$YH$



**Table 4 (cont) Transactions Relationships for a Global CGE Model**

	<b>Government</b>	<b>Investment</b>	<b>Margins</b>	<b>RoW</b>
<b>Commodities</b>	$(PQD_c * QGD_c)$	$(PQD_c * QINVD_c)$	$\begin{pmatrix} PWE_{c,w} * QER_{c,w} \\ *ER \end{pmatrix}$	$\begin{pmatrix} PWE_{c,w} * QER_{c,w} \\ *ER \end{pmatrix}$
<b>Activities</b>	0	0	0	0
<b>Factors</b>	0	0	0	0
<b>Households</b>	0	0	0	0
<b>Government</b>	0	0	0	0
<b>Savings</b>	$(YG - EG)$	0	$(KAPREG * ER)$	$(KAPREG * ER)$
<b>Margins</b>	0	0	0	0
<b>Rest of World</b>	0	0	0	0
<b>Total</b>	$YG$	$INVEST$	0	0

## 3.2 Price and Quantity Systems for a Representative Region

### 3.2.1 Price System

The price system is built up using the principle that the components of the ‘price definitions’ for each region are the entries in the columns of the SAM. Hence there are a series of explicit accounting identities that define the relationships between the prices and thereby determine the processes used to calibrate the tax rates for the base solution. However, the model is set up using a series of linear homogeneous relationships and hence is only defined in terms of relative prices. Consequently, as part of the calibration process it is necessary set some of the prices equal to one (or any other number that suits the modeller) – this model adopts the convention that prices are normalised at the level of the CES and CET aggregator functions  $PQS$ , the supply price of the domestic composite consumption commodity and  $PXC$ , the producer price of the composite domestic output. This is the nearest equivalent to basic prices available in the GTAP database. The price system for a typical region in a 4-region global model is illustrated by Figure 1 – note that this representation abstracts from the Globe region.



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quantity imported from the source region is a ‘large’ share of the commodity imported then the composite import price ( $PML$ ) is a CES aggregate of the prices from the source regions. On the other hand, if the quantity imported from the source region is a ‘small’ share of the commodity imported then the composite import price ( $PMS$ ) is a Leontief aggregate of the prices from the source regions.<sup>8</sup> The user can adjust the definition of a ‘small’ source region when configuring the model; the definition of a ‘large’ source region is then defined as the complement. The region specific import prices are expressed in terms of the domestic currency units after paying for trade and transport services and any import duties. Thus a destination region is assumed to purchase a commodity in a source economy where the price is defined in “world dollars” at the basket exchange rate and is valued free on board ( $fob$ ), i.e.,  $PWMFOB$ . The carriage insurance and freight ( $cif$ ) price ( $PWM$ ) is then defined as the  $fob$  price plus trade and transport margin services ( $margcor$ ) times the unit price of margin services ( $PT$ ). The  $cif$  prices are related to the domestic price of imports by the addition of any import duties ( $TM$ ) and then converted into domestic currency units using the nominal exchange rate ( $ER$ ).

The prices for commodities by activities ( $PXC$ ) are determined by the domestic prices ( $PD$ ) and the composite export prices ( $PE$ ). The composite export prices are a CET aggregates of the export prices received by the source economy for exports to specific destinations ( $PER$ ). The prices of the composite exports are determined as aggregates of the domestic prices paid for exports by all those regions that demand exports from this economy under the maintained assumption that exports are differentiated both by their destination region and the ‘regional’ group that the destination region is part of; hence there is a two-stage sub aggregation process whereby exports to like groups so regions are aggregated to form intermediate aggregates of exported commodities, which are then aggregated to form the composite export commodities. This allows for a degree of differentiation by both destination and commodity. The prices paid by the destination regions ( $PWE$ ) are net of export taxes ( $TE$ ) and are expressed in the currency units of the model’s reference region by use of the nominal exchange. Notice how the export prices by region of destination ( $PER$ ), and the intermediate aggregates, are all normalised on 1, but the seeming counterpart of normalising import prices by source region ( $PMR$ ) are not normalised on 1. The link between the regions is therefore embedded in the identification of the quantities exchanged rather than the normalised prices

<sup>8</sup> The impact of adding an additional level of nesting is explored in McDonald and Thierfelder (2006).

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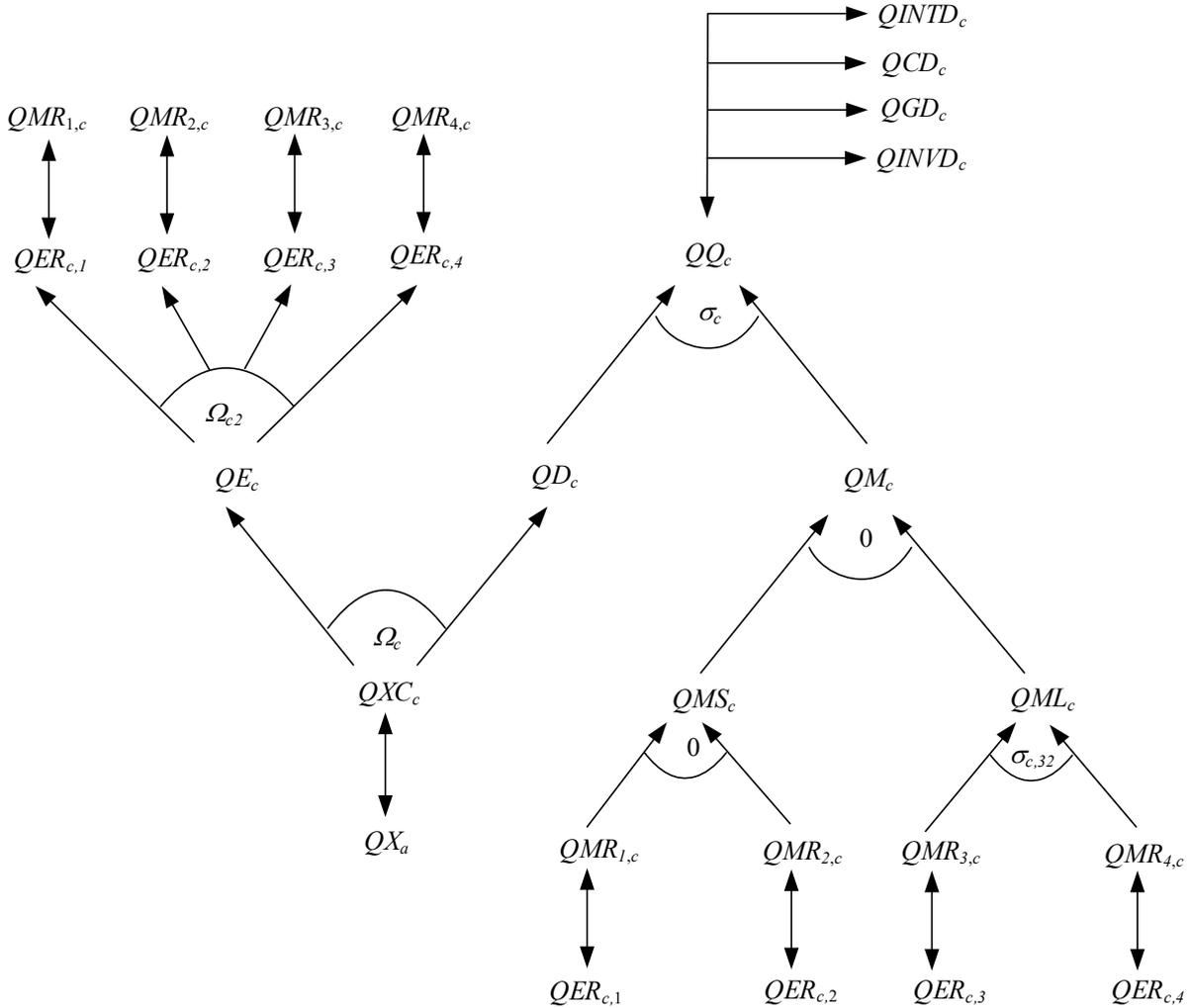
and is a natural consequence of the normalisation process. The CET function can be switched off so that the domestic and export commodities are assumed to be perfect substitutes; this is the assumption in the GTAP model and is an option in this model.

The price system also contains a series of equilibrium identities. Namely the *fob* export price (*PWE*) for region *s* on its exports to region *d* must be identical to the *fob* import price (*PWMFOB*) paid by region *d* on its imports from region *s*. These equilibrium identities are indicated by double headed arrows.

### 3.2.2 Quantity System

The quantity system for a representative region is somewhat simpler. The composite consumption commodity (*QQ*) is a mix of the domestically produced commodity (*QD*) and the composite import commodity (*QM*), where the domestic and imported commodities are imperfect substitutes, and the imported commodities are differentiated by their source region via a two-stage sub aggregation process whereby imports are differentiated by reference to their shares in the imports of that commodity by the destination region. The composite imported commodity is a Leontief aggregate of the composite imports from regions with ‘small’ (*QMS*) and ‘large’ (*QML*) import shares. *QMS* is a Leontief aggregate of the imports from source regions with ‘small’ import share while *QML* is a CES aggregate of imports from source regions with ‘large’ import shares. The equilibrium conditions require that the quantities imported from different regions (*QMR*) are identical to the quantities exported by other regions to the representative region (*QER*).

**Figure 2**                      **Quantity System for a Typical Region**



The composite consumption commodity is then allocated between domestic intermediate demands ( $QINTD$ ), private consumption demand ( $QCD$ ), government demand ( $QGD$ ) and investment demand ( $QINVD$ ).

On the output side, domestic output by activity ( $QX$ ) is identical to domestic commodity output ( $QXC$ ). Domestically produced commodities are then allocated between the domestic market ( $QD$ ) and composite export commodities ( $QE$ ) under the maintained assumption of imperfect transformation. Exports are allocated between the different destination regions ( $QER$ ) under the maintain assumption of imperfect transformation.

### 3.2.3 Production System

The three level production developed was widely adopted by the early 2000s and was increasingly common by the first half of the 2010s. The method developed here is flexible and is a simplification of the generalised production system used in recent, post 2016, versions of the STAGE and ANARRES models.<sup>9</sup> The generalised system can contain  $n$ -levels and can be used to include substitution possibilities that include primary and intermediate inputs, e.g., in energy, climate, water, etc., models. The method depends upon the inclusion of appropriate set definitions and mapping sets with minimal need to change the models equations, but it can be easy to make mistakes and not so easy to identify the mistakes. For this model the production system is limited to three levels: this is consistent with a pedagogic method involving sequential elaboration.

The production system is set up as a three-level nest of CES production functions. At the top level aggregate intermediate inputs ( $QINT$ ) are combined with aggregate primary inputs ( $QVA$ ) to produce the output of an activity ( $QX$ ). This top level production function can take either CES or Leontief form, with CES being the default and the elasticities being activity **and** region specific.<sup>10</sup> Aggregate intermediate inputs are a Leontief aggregation of the individual intermediate inputs where the input-output coefficients ( $ioqint$ ) are defined in terms of input quantities relative to the aggregate intermediate input.<sup>11</sup> The value added production function is a standard CES function over capital, land, natural resources and **aggregate** labour, with the elasticities being activity **and** region specific. The set of primary inputs ( $ff$ ) includes all the natural primary inputs in GTAP (capital, land, natural resources and skilled and unskilled labour) plus aggregate labour, where the natural inputs make up the set  $f$ , i.e., the set  $ff$  is the union of the set  $f$  and aggregate labour. The notation for all primary inputs, natural and aggregates, is the same: quantity demand is  $FD$ , quantity supplied is  $FS$  and the factor prices is  $WF$ . The operation of this aggregator function can, of course, be influenced by choices over the closure rules for the factor accounts.

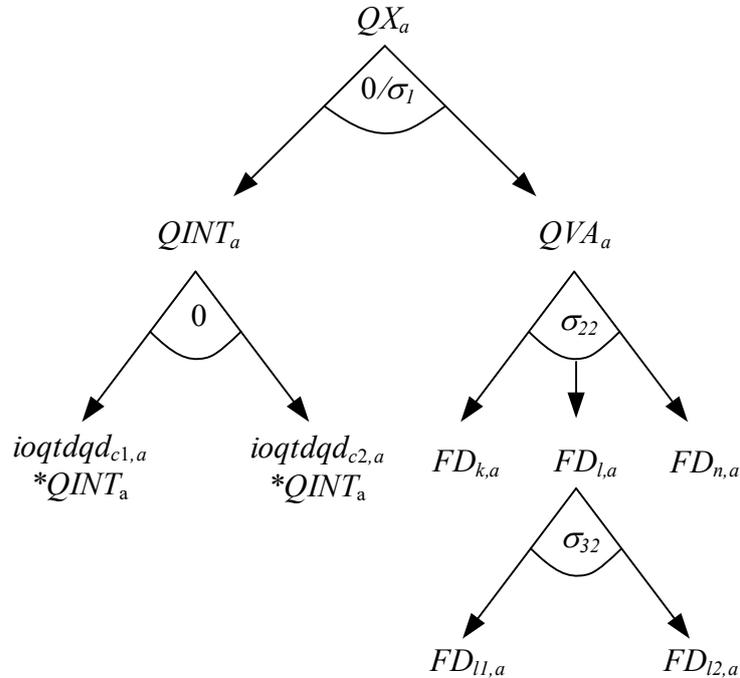
<sup>9</sup> Prior to the development of this generalised system the STAGE and GLOBE/ANARRES models were ‘hard coded’ where each level of the nests was represented by primal and first-order conditions. Changes to the nested system required changes, sometimes extensive, to the model equations and calibration systems.

<sup>10</sup> The model allows the user to specify the share of intermediate input cost in total cost below which the Leontief alternative is automatically selected. The user also has the option to make activity and region-specific decisions about the selection of CES or Leontief forms.

<sup>11</sup> A more flexible specification exists but is not included in the ‘standard’ version of ANARRES\_t.

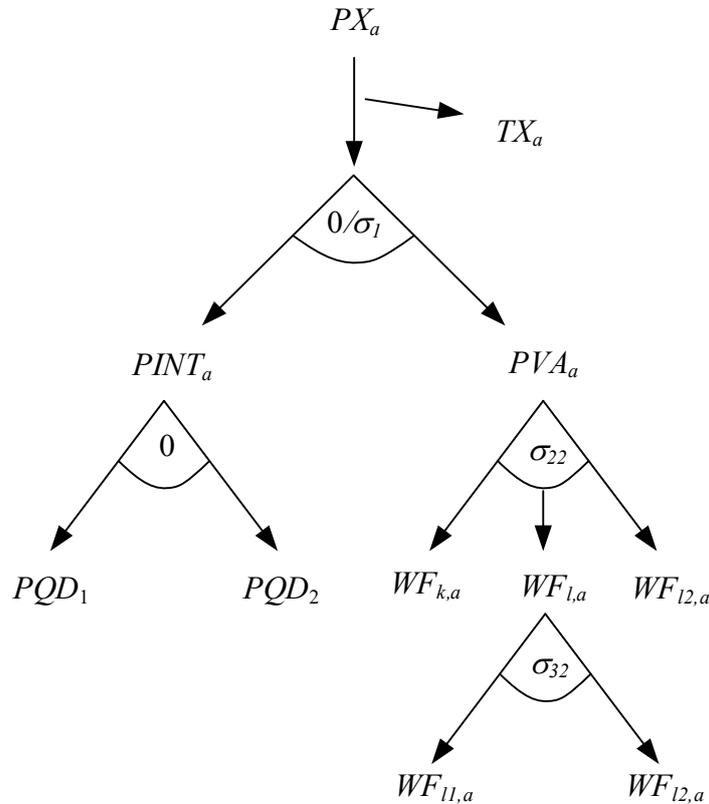
The allocation of the finite supplies of factors (*FS*) between competing activities depends upon relative factor prices via first order conditions for optima.

**Figure 3 Three Level Production System: Quantities**



The price relations for the production system are illustrated in Figure 4. Note how the prices paid for intermediate inputs (*PQD*) are the same as paid for final demands, i.e., a ‘law’ of one price relationship holds across all domestic demand. Note also that factor prices are factor and activity specific ( $WFA_{f,a}$ ); in the model  $WFA_{f,a} = WF_f * WDIST_{f,a}$ , i.e., the labels used in Figure 4 are ‘abbreviations’. In the price system for production the value added prices (*PVA*) are determined by the activity prices (*PX*), the production tax rates (*TX*), the input-output coefficients (*ioqint*) and the commodity prices (*PQD*). The price of value added is determined by the factor prices (*WF*) and any factor use taxes (*tf*). The activity prices are a one to one mapping of the commodity prices received by activities (*PXC*); this is a consequence of the supply matrix being a square diagonal matrix.

**Figure 4 Two Level Production System: Prices**



**3 The Globe Region**

An important feature of the model is the use of the concept of a region known as Globe. While the GTAP database contains complete bilateral information relating to the trade in commodities, i.e., in all cases transactions are identified according to their region of origin and their region of destination, this is not the case for trade in margins services associated with the transportation of commodities. Rather the GTAP database identifies the demand, in value terms, for margin services associated with imports by all regions from all other regions but does not identify the region that supplies the margin services associated with any specific transaction. Consequently, the data for the demand side for margin services is relatively detailed but the supply side is not. Indeed, the only supply side information is the total value of exports of margin services by each region. The Globe construct allows the model to get around this shortage of information, while simultaneously providing a general method for dealing with any other transactions data where full bilateral information is missing.



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assumed to be differentiated by source region and the proportion of imports accounted for by the source region. Thus a two-level Leontief and CES aggregation nest is used. It is assumed that imports of trade and transport services can *potentially* incur trade and transport margins (*margcor*) and face tariffs (*TM*); in fact, the database does not include any transport margins or tariff data for margin services in relation to the destination region, although they can, and do, incur export taxes levied by the exporting region.

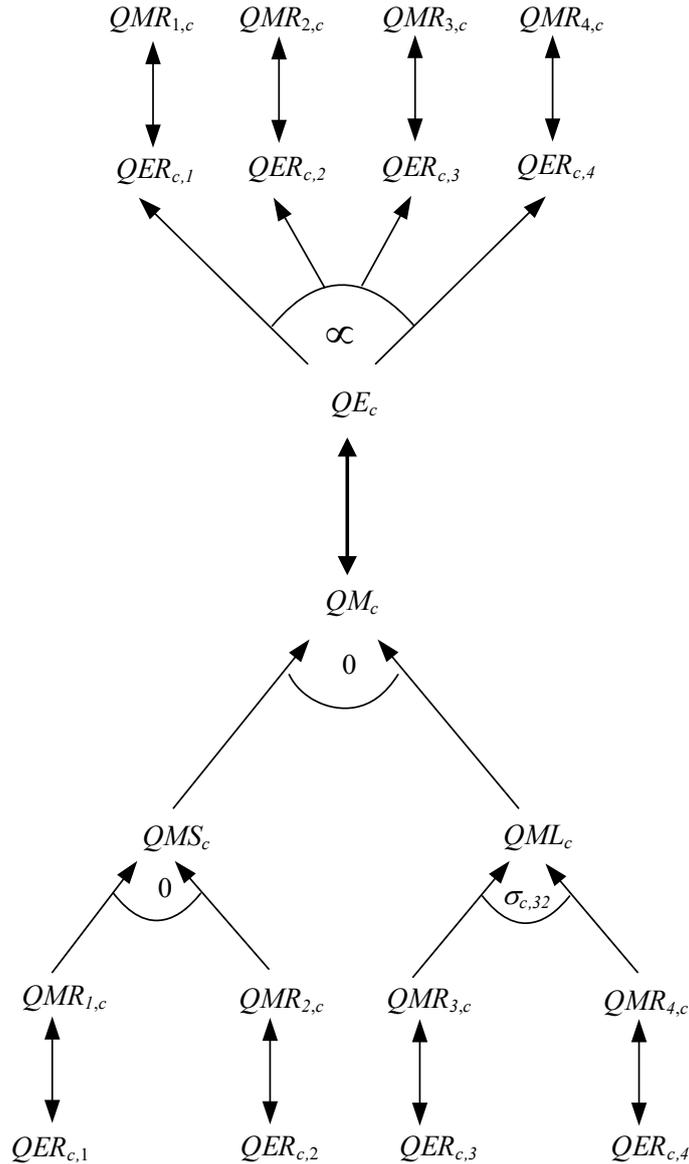
The export side is slightly different. In effect the Globe region is operating as a method for pooling differentiated commodities used in trade and transport services and the only differences in the use of trade and transport services associated with any specific import are the quantities of each type of trade service used and the mix of types of trade services. Underlying this is the implicit assumption that each type of trade service used is homogenous, and should be sold therefore at the same price. Hence the export price system for Globe needs to be arranged so that Globe exports at a single price, i.e., there should be an infinite elasticity of substitution between each type of trade service exported irrespective of its destination region. Therefore, the average export price (*PE*) should equal the price paid by each destination region (*PER*), which should equal the export price in world currency units (*PWE*) and will be common across all destinations (*PT*).

The linked quantity system contains the same asymmetry in the treatment of imports and exports by Globe (see Figure 6). The imports of trade and transport commodities are assumed to be differentiated by region and the proportion of imports accounted for by the source region, hence the elasticity of substitution is greater than or equal to zero but less than infinity, while the exports of trade and transport commodities are assumed to be homogenous and hence the elasticities of transformation are infinite.

One consequence of using a Globe region for trade and transport services is that Globe runs trade balances with all other regions. These trade balances relate to the differences in the values of trade and transport commodities imported from Globe and the value of trade and transport commodities exported to Globe; however, the sum of Globe's trade balances with other regions must be zero since Globe is an artificial construct rather than a real region. But the demand for trade and transport services by any region is determined by technology, i.e., the coefficients *margcor*, and the volume of imports demanded by the destination region. This means that the prices of trade and transport commodities only have an indirect effect upon

their demand – the only place these prices enter into the import decision as a variable is as a partial determinant of the difference between the *fob* and *cif* valuations of other imported commodities. Consequently, the primary market clearing mechanism for the Globe region comes through the quantity of trade and transport commodities it chooses to import.

**Figure 6**                    **Quantity System for the Globe Region**



The Globe concept has other potential uses in the model. All transactions between regions for which there is an absence of full bilateral information can be routed through the Globe region. While this is not a ‘first best’ solution, it does provide a ‘second best’ method by which augmented versions of the GTAP database can be used to enrich the analyses of

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international trade in a global model prior to availability of full bilateral transactions data (see McDonald and Sonmez (2006) for and application).

## 4. Formal Description of the Model

This formal description of the model proceeds in five stages with three of them in this section and the fourth, relating to model closure rules, being detailed in the next section. The fifth stage is in Appendix A1 where alternative specifications for the Armington and CET functions are detailed. For this section the description begins with identification of the sets used in the model, this is followed by details of each equation (block) in the model and ends with a table that summarises all the equations and identifies the associated variables, the counts for equations and variables and identifies whether the equation is implemented or not for the Globe region.

### 4.1 Model Sets

Rather than writing out each and every equation in detail it is useful to start by defining a series of sets; thereafter if a behavioural relationship applies to all members of a set an equation only needs to be specified once. The natural choice for this model is a set for all the transactions by each region (*sac*) plus a series of sets that group commodities, activities, factors, import duties, export taxes, trade margins, trade and finally some individual accounts relating to domestic institutions. The outer set for any region is defined as

$$sac = \{c, a, f, h, tmr, tmrs, ter, tff, g, i, owatpmarg, w, total\}$$

and the following are the basic sets for each region in this model

- $c(sac) = \{\text{commodities}\}$
- $a(sac) = \{\text{activities}\}$
- $ff(sac) = \{\text{natural and aggregate factors}\}$
- $f(ff) = \{\text{natural factors}\}$
- $h(sac) = \{\text{household}\}$
- $tmr(sac) = \{\text{ad valorem import duties}\}$
- $tmrs(sac) = \{\text{specific import duties}\}$
- $ter(sac) = \{\text{export taxes}\}$
- $tff(sac) = \{\text{factor use taxes}\}$
- $g(sac) = \{\text{saltax, vattax, prodtax, facttax, dirtax, govt}\}$
- $i(sac) = \{i_s\}$
- $owatpm\ arg(sac) = \{\text{trade and transport margins}\}$
- $w(sac) = \{\text{rest of the world - trade partners and aggregates}\}$

Various subsets of  $a$  and  $c$  are declared and then assigned on the basis of certain characteristics of the data set used to calibrate the specific implementation of the model, so-called dynamic sets. The subsets of  $a$  used in the model are

- $acx(a, r) = \{\text{activities purchased domestically}\}$
- $acxn(a, r) = \{\text{activities NOT purchased domestically}\}$
- $aqx(a, r) = \{\text{Activities with CES function at Level 1 of nest}\}$
- $aqxn(a, r) = \{\text{Activities with Leontief function at Level 1 of nest}\}$
- $aleon(a) = \{\text{activities with Leontief top level prodn function}\}$

while the subsets of  $c$  used in this model are

- $ct(c, r) = \{\text{trade margin commodities}\}$
- $ctn(c, r) = \{\text{non-trade margin commodities}\}$
- $ct2(c, r) = \{\text{trade margin commodities used for Globe}\}$
- $ctn2(c, r) = \{\text{non-trade margin commodities used for Globe}\}$
- $ce(c, r) = \{\text{export commodities}\}$
- $cen(c, r) = \{\text{non-export commodities}\}$
- $cer(c, r, w) = \{\text{export commodities by region}\}$
- $cern(c, r, w) = \{\text{non-export commodities by region}\}$
- $cm(c, r) = \{\text{imported commodities}\}$
- $cmn(c, r) = \{\text{non-imported commodities}\}$
- $cmr(w, c, r) = \{\text{imported commodities by region}\}$
- $cmrn(w, c, r) = \{\text{non-imported commodities by region}\}$
- $cmrs(w, c, r) = \{\text{small shares imported commodities by aggregate region}\}$
- $cmrsn(w, c, r) = \{\text{non-small shares imported commodities by aggregate region}\}$
- $cms(c, r) = \{\text{commodities small shares}\}$
- $cmrl(w, c, r) = \{\text{large shares imported commodities by aggregate region}\}$
- $cmrln(w, c, r) = \{\text{non-large shares imported commodities by aggregate region}\}$
- $cml(c, r) = \{\text{commodities large shares}\}$
- $cmrn2(c, r, w) = \{\text{non-imported commodities by aggregate region}\}$
- $cx(c, r) = \{\text{commodities produced domestically}\}$
- $cxn(c, r) = \{\text{commodities NOT produced domestically AND imported}\}$
- $cd(c, r) = \{\text{commodities produced AND demanded domestically}\}$
- $cdn(c, r) = \{\text{commodities NOT produced AND demanded domestically}\}$
- $cintd(c, r) = \{\text{commodities WITH intermediate demand by region}\}$
- $cintdn(c, r) = \{\text{commodities WITHOUT intermediate demand by region}\}$

and a subset of  $w$  is needed to allow for Globe

$$wgn(w) = \{\text{Rest of world without Globe}\}.$$

It is also necessary to define a set of regions,  $r$ , for which there are two subsets

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$$\begin{aligned}
 rgn(r) &= \{\text{all regions excluding Globe}\} \\
 ref(r) &= \{\text{reference regions for global numeraire}\} \\
 rleon(r) &= \{\text{regions with Leontief top level prodn function}\}
 \end{aligned}$$

A macro SAM that facilitates checking various aspects of model calibration and operation is used in the model and this needs another set, *ss*,

$$ss = \left\{ \begin{array}{l} \text{commdty, activity, valuat, hholds,} \\ \text{tmtax, tetax, govtn, kapital, margs, world, totals} \end{array} \right\}.$$

The model also makes use of a series of mapping files that are used to link sets. These are

$$\begin{aligned}
 map\_w\_tmr(w, tmr) &= \{\text{Ad valorem tariff mapping}\} \\
 map\_tmr\_w(tmr, w) &= \{\text{Ad valorem tariff mapping reverse}\} \\
 map\_w\_tmrs(w, tmrs) &= \{\text{Specific tariff mapping}\} \\
 map\_tmrs\_w(tmrs, w) &= \{\text{Specific tariff mapping reverse}\} \\
 map\_w\_ter(w, ter) &= \{\text{Export tax mapping}\} \\
 map\_ter\_w(ter, w) &= \{\text{Export tax mapping reverse}\} \\
 map\_c\_w\_marg(c, w, owatpmarg) &= \{\text{Trade margin mapping of owatpmarg to ct2 and w}\} \\
 map\_marg\_w(owatpmarg, w) &= \{\text{Trade margin mapping of w to owatpmarg}\} \\
 mapr\_w(r, w) &= \{\text{Region to trade partner mapping}\} \\
 mapw\_r(w, r) &= \{\text{Region to trade partner mapping}\} \\
 map\_f\_tff(f, tff) &= \{\text{Factor taxes to factors}\} \\
 map\_tff\_f(tff, ff) &= \{\text{Factor taxes to factors reverse}\} \\
 map\_aagg\_a(aagg, a) &= \{\text{Mapping from activities to aggregate activities}\} \\
 map\_cagg\_c(cagg, c) &= \{\text{Mapping from commodities to aggregate commodities}\} \\
 map\_wagg\_w(wagg, w) &= \{\text{Mapping from regions to aggregate regions}\} \\
 map\_ragg\_r(ragg, r) &= \{\text{Mapping from regions to aggregate regions}\}
 \end{aligned}$$

Finally various other sets are declared to facilitate model operation. These are

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$sacn(sac) = \{\text{SAM accounts without totals}\}$

$ssn(ss) = \{\text{Macro SAM accounts without totals}\}$

$cons = \{\text{set for programme control parameters}\}$

#### 4.1.1 Reserved Names

The model uses a number of names that are reserved; these are

dirtax	Direct Taxes
saltax	Sales Taxes
vattax	Value Added Taxes
prodtax	Production Taxes
factax	Factor Taxes

#### 4.1.2 Conventions

The equations for the model are set out in 11 ‘blocks’ each of which can contain a number of sub blocks. The equations are grouped under the following headings:

1. TRADE BLOCK
  - a. Exports Block
  - b. Imports Block
2. COMMODITY PRICE BLOCK
3. NUMERAIRE PRICE BLOCK
4. PRODUCTION BLOCK
  - a. Production
  - b. Intermediate Input Demand
  - c. Commodity Output
  - d. Activity Output
5. FACTOR BLOCK
6. HOUSEHOLD BLOCK
  - a. Household Income
  - b. Household Expenditure
7. GOVERNMENT BLOCK
  - a. Government Tax Rates
  - b. Government Tax Revenues
  - c. Government Income

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- d. Government Expenditure Block
- 8. KAPITAL BLOCK
  - a. Savings Block
  - b. Investment Block
- 9. MARKET CLEARING BLOCK
  - a. Factor Accounts
  - b. Commodity Accounts
  - c. Commodity Trade Accounts
  - d. Margin Trade Accounts
- 10. MACROECONOMIC CLOSURE BLOCK
  - a. Investment and Savings Accounts
  - b. Absorption Closure
- 11. MACROECONOMIC AGGREGATES BLOCK
- 12. SLACKS BLOCK

This grouping is carried throughout the model code, i.e., it is followed for the parameter declaration and calibration, variable declaration and variable initialization sections. This modularization of the code is adopted for ease of reading and altering the model rather than being a requirement of the model.

A series of conventions are adopted for the naming of variables and parameters. These conventions are not a requirement of the modelling language; rather they are designed to ease reading of the model.

- All VARIABLES are in upper case.
- The standard prefixes for variable names are:  $P$  for price variables,  $Q$  for quantity variables,  $W$  for factor prices,  $F$  for factor quantities,  $E$  for expenditure variables,  $Y$  for income variables, and  $V$  for value variables
- All variables have a matching parameter that identifies the value of the variable in the base period. These parameters are in upper case and carry a '0' suffix, and are used to initialise variables.
- A series of variables are declared that allow for the equiproportionate multiplicative adjustment of groups of variables. These variables are named using the convention  $**ADJ$ , where  $**$  is the variable series they adjust.

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- A series of variables are declared that allow for the additive adjustment of groups of variables. These variables are named using the convention  $D^{**}$ , where  $**$  is the variable series they adjust.
- All parameters are in lower case, except those paired to variables that are used to initialise variables.
- Parameter names have a two or five-character suffix which distinguishes their definition, e.g.,  $**sh$  is a share parameter,  $**av$  is an average and  $**const$  is a constant parameter.
- For the Armington (CES) functions all the share parameters are declared with the form  $delta^{**}$ , all the shift/efficiency parameters are declared with the form  $ac^{**}$ , and all the elasticity parameters are declared with the form  $rho^{**}$ , where  $**$  identifies the function in which the parameter operates.
- For the CET functions all the share parameters are declared with the form  $gamma^{**}$ , all the shift/efficiency parameters are declared with the form  $at^{**}$ , and all the elasticity parameters are declared with the form  $rho^{**}$ , where  $**$  identifies the function in which the parameter operates.
- All coefficients in the model are declared with the form  $io^{****}$ , where  $****$  consists of two parts that identify the two variables related by the coefficient.
- The index ordering follows the specification in the SAM: row, column, and then  $r$  to indicate the region. For example, exports from region  $r$  to region  $w$  would be  $QER_{c,w,r}$  because region  $r$ 's export data in its SAM is found in the commodity row ( $c$ ) and the trade partner column ( $w$ ). Likewise, imports in region  $r$  from region  $w$  are designated,  $QMR_{w,c,r}$  because region  $r$ 's import data in its SAM is found in the trade partner row ( $w$ ) and the commodity column ( $c$ ).
- All sets have another name, or alias, given by the set name followed by "p". For example, the set of commodities may be called  $c$  or  $cp$ .

## 4.2 Equations for the Model

The model equations are reported and described by blocks/groups below and then they are summarised in table A4 in the appendix.

#### 4.2.1 Exports Block Equations

The treatment of exports is complicated by the incorporation of the facility to treat export commodities as imperfect and by the need to accommodate the special case of exports (of trade and transport services) that are homogenous from Globe. The presumption of imperfect substitution is the default presumption in this model; reasons for this decision being its symmetry with the Armington assumption on the imports side, the amelioration of the terms of trade effects associated with the Armington assumption and a belief that in general there is differentiation between commodities supplied to domestic and export markets. However, there are proponents of the arguments for treating exports as perfect substitutes and there are clearly cases where such an assumption may be appropriate, e.g., supplies of unprocessed mineral products.<sup>12</sup> A formulation of the model allows the CET functions to be switched off at either or both levels of the export supply nest for specific commodities and/or for specific regions.

The domestic prices of commodity exports,  $c$ , by destination,  $w$ , and source,  $r$ , region ( $PER$ ) are defined as the product of world prices of exports ( $PWE$ ) – also defined by commodity and destination and source region, the source region's exchange rate ( $ER$ ) and one minus the export tax rate ( $TE$ )<sup>13</sup> ( $X1$ ). The possibility of non-traded commodities means that the equations for the domestic prices of exports (and imports) are only implemented for those commodities that are traded; this requires the use of a dynamic set,  $cer$ , which is defined by those commodities that are exported in the base data. Also notice that the concept of a single world price for a commodity is a valid concept since, by definition, world prices are endogenous and therefore ALL regions are treated as 'large' producers of a commodity. Hence an extreme version of the small country assumption is not supported but the shares of total exports of a commodity accounted for by each region will be a determinant of each region's impact on the average world price.

<sup>12</sup> The GTAP model assumes perfect substitution and historically it has been argued that perfect substitution is appropriate for Australia. It has been argued that the use of CET functions for exports can be avoided by increasing the degree of disaggregation, however, as a rule, this is not appropriate for models calibrated to the GTAP database because the commodity accounts are fixed. This argument also lacks symmetry since the same argument could be adopted with respect to imports and the Armington assumption. There are however reasons to be cautious about the use of CET function (see McDonald, 2011).

<sup>13</sup> In the ANARRES model ALL taxes are expressed as having positive values; any tax rate with a negative value is a subsidy rate.

**Export Block Equations 1**

$$PER_{c,w,r} = PWE_{c,w,r} * ER_r * (1 - TE_{c,w,r}) \quad \forall c \in cer \quad (X1)$$

$$PE_{c,r} * QE_{c,r} = \sum_w PER_{c,w,r} * QER_{c,w,r} \quad \forall c \in ce, r \in rgn \quad (X2)$$

$$PER_{c,w,r} = PE_{c,r} \quad \forall c \in ct2, r \notin rgn, w \in wgn \quad (X3)$$

$$QXC_{c,r} = at_{c,r} * \left( \gamma_{c,r} * QE_{c,r}^{\rho_{c,r}^t} + (1 - \gamma_{c,r}) * QD_{c,r}^{\rho_{c,r}^t} \right)^{1/\rho_{c,r}^t} \quad (X4)$$

$\forall c \in (cd \cap ce), r \in rgn$

$$QE_{c,r} = QD_{c,r} \left[ \frac{PE_{c,r}}{PD_{c,r}} * \frac{(1 - \gamma_{c,r})}{\gamma_{c,r}} \right]^{\frac{1}{(\rho_{c,r}^t - 1)}} \quad \forall c \in (cd \cap ce), r \in rgn \quad (X5)$$

$$QXC_{c,r} = QD_{c,r} + QE_{c,r} \quad \forall (c \in (cd \cap cen), r \in rgn)$$

OR  $\forall (c \in (cdn \cap ce), r \in rgn)$  (X6)

The prices of the composite export commodities can then be expressed as simple volume weighted averages of the export prices by region, where  $PE_{c,r}$  and  $QE_{c,r}$  the price and quantity of the composite export commodity  $c$  from region  $r$ , and the weights are the volume shares of exports and are variable. This comes from the fact that a CET function is linear homogenous and hence Eulers theorem can be applied. Notice however that (X2) is only implemented of the set  $rgn$ , i.e., the region Globe is excluded. Rather the composite export price for trade margin commodities from Globe is defined in X3, which indicates that it is assumed that the trade margin commodities exported by Globe are perfect substitutes for each other, i.e., the same price is paid for each trade margin commodity by ALL purchasing regions.

Domestic commodity outputs ( $QXC$ ) are either exported ( $QE$ ) as composite commodities or supplied to the domestic market ( $QD$ ). The allocation of output between the domestic and export markets is determined by the output transformation functions, Constant Elasticity of Transformation (CET) functions, (X4) with the optimum combinations of  $QE$  and  $QD$  determined by first-order conditions (X5). In this version of the model primal forms of the CET are used with associated first-order conditions. However, some commodities are

non-traded and therefore X4 and X5 are implemented if and only if the commodity is traded. This means that domestic commodity outputs are undefined for non-traded commodities, but by definition the quantity supplied to the domestic market is the amount produced, and it is necessary to cover the possibility that a commodity may be produced domestically and exported but not consumed domestically. These two sets of possibilities are covered by X6.

### **Export Block Equations 2**

$$QER_{c,w,r} = QE_{c,r} * \left( \frac{PER_{c,w,r}}{\left( (PE_{c,r} * \gamma_{c,w,r}^r * at_{c,r}^r)^{\rho_{c,r}^e} \right)} \right)^{\left( \frac{1}{(\rho_{c,r}^e - 1)} \right)} \quad \forall c \in cer2, r \in rgn \quad (X7)$$

$$QE_{c,r} = \sum_w QER_{c,w,r} \quad \forall c \in ct, r \notin rgn. \quad (X8)$$

$$QE_{c,r} = QM_{c,r} \quad \forall c \in ct2, r \notin rgn. \quad (X9)$$

These quantity equations deal however only with the composite export commodities, i.e., hypothetical commodities whose roles in the model are to act as neutral intermediaries that enter into the first-order conditions that determine the optimal mix between domestic use and exports of domestic commodity production (X5). In the model the composite export commodities are themselves CET aggregates of commodity exports to different regions (*QER*), and the appropriate first order condition is given by (X7). Initially the formulation of X7 is not intuitive but, as demonstrated in Appendix A1, the formulation is a straightforward manipulation of a more conventional representation; this form is used because it improves model performance. Note however that (X7) does not define the exports of trade margin commodities BY Globe; this is because these commodities are assumed to be perfect substitutes and therefore simple addition is adequate, this is done by X8.

Finally, there is a need for an equilibrium conditions for trade by Globe. Since Globe is an artificial construct whose sole role in the model is to gather exports whose destinations are unknown and supply imports whose sources are unknown, and vice versa, it must always balance its trade within each period. Thus the volume of exports of trade margin commodities

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by Globe must be exactly equal to the volume of imports of trade margin commodities, see X9.

#### 4.2.2 Imports Block Equations

The prices of imported commodities are made up of several components. The export price in foreign currency units – valued free on board (*job*) (*PWMFOB*) – plus the cost of trade and transport services, which gives the import price carriage insurance and freight (*cif*) paid (*PWM*), plus any import duties; all of which are then converted into domestic currency units (*PMR*). Clearly the import price value *job* (*PWMFOB*) is identical to the export price valued *job* (*PWE*) – this condition is imposed in the market clearing block (see below) – and hence the *cif* price is defined in M3, where *margcor* is the quantity of trade and transport services required to import a unit of the imported commodity and *PT* is the price of trade and transport services. Embedded in the definition of the coefficient *margcor* is the explicit assumption that transporting a commodity from a specific source to a specific destination requires the use of a specific quantity of services – the actual cost of these services can vary according to changes in the prices of the trade and transport services, or the quantity of services required to transport a particular commodity.

The domestic prices of imports from a region (*PMR*) are then defined as the product of world prices of imports (*PWM*) – after payment for carriage, insurance and freight (*cif*) - the exchange rate (*ER*) and one plus the *ad valorem* import tariff rate (*TM*) plus any (quantity) specific import duty (*TMS*). The possibility of non-traded commodities means that the equations for the domestic prices of imports are only implemented for those commodities that are traded; this requires the use of a dynamic set, *cmr*, which is defined by those commodities that are imported by a region from another region in the base data.

### Import Block Equations 1

$$PML_{c,r} = \frac{\sum_{w \in cml_{w,c,r}} (PMR_{w,c,r} * QMR_{w,c,r})}{QML_{c,r}} \quad \forall (c,r) \in cml \quad (M1)$$

$$PMS_{c,r} = \sum_w ioqmrqms_{w,c,r} * PMR_{w,c,r} \quad \forall (c,r) \in cms \quad (M2)$$

$$PWM_{w,c,r} = PWMFOB_{w,c,r} + \left( \sum_{cp \in cl_{cp,r}} margcor_{w,cp,c,r} * PT_{cp,r} \right) \quad (M3)$$

$\forall c \in cmr$

$$PMR_{w,c,r} = PWM_{w,c,r} * ER_r * (1 + TM_{w,c,r}) + TMS_{w,c,r} \quad \forall c \in cmr . \quad (M4)$$

$$PM_{c,r} * QM_{c,r} = (PML_{c,r} * QML_{c,r}) + (PMS_{c,r} * QMS_{c,r}) \quad (M5)$$

$\forall (c,r) \in cm_{c,r}$

The model treats imports that account for ‘small’ shares of imports of a commodity by a region differently from those that account for ‘large’ shares of imports of a commodity by a region.<sup>14</sup> This is because the operations of CES, and CET, functions depend not only on the elasticity of substitution but also on the shares of the arguments: commodities with ‘small’ trade shares can have a disproportionately large impact on the terms of trade in such aggregation functions. For commodities with ‘small’ trade shares it is assumed that they account for fixed proportions ( $ioqmrqms_{w,c,r}$ ) of the total volume of imports of a commodity: the justification for this assumption rest upon a (vaguely defined) specific factor specification. The composite price of ‘small’ share imports ( $PMS$ ) is therefore a quantity share weighted aggregate of the landed prices (M2). The composite price of ‘large’ share imports ( $PML$ ) is a simple volume weighted averages of the of the import prices by region: this derives from the fact that a CES function is liner homogenous and hence Eulers theorem can be applied (M1).

<sup>14</sup> The definition of ‘small’, and hence by complement ‘large’, is selected by the user when calibrating the model.

**Import Block Equations 2**

$$QQ_{c,r} = ac_{c,r} \left( \delta_{c,r} * QM_{c,r}^{-\rho_{c,r}^c} + (1 - \delta_{c,r}) * QD_{c,r}^{-\rho_{c,r}^c} \right)^{\left( \frac{1}{\rho_{c,r}^c} \right)} \quad \forall c \in (cx \cap cm), r \in rgn \quad (M6)$$

$$QM_{c,r} = QD_{c,r} * \left( \left( \frac{PD_{c,r}}{PM_{c,r}} \right) * \left( \frac{\delta_{c,r}}{(1 - \delta_{c,r})} \right) \right)^{\frac{1}{(1 + \rho_{c,r}^c)}} \quad \forall c \in (cx \cap cm), r \in rgn \quad (M7)$$

$$QQ_{c,r} = QD_{c,r} + QM_{c,r} \quad \forall c \in (cx \cap cmn), r \in rgn \quad (M8)$$

OR  $\forall c \in (cxn \cap cm), r \in rgn$

$$QMS_{c,r} = ioqmsqm_{c,r} + QM_{c,r} \quad \forall c \in cms \quad (M9)$$

$$QML_{c,r} = ioqmlqm_{c,r} + QM_{c,r} \quad \forall c \in cml \quad (M10)$$

$$QMR_{w,c,r} = ioqmrqms_{w,c,r} + QMS_{c,r} \quad \forall c \in cmrs \quad (M11)$$

$$QMR_{w,c,r} = QML_{c,r} * \left( \frac{PMR_{w,c,r} * acr_{c,r}^{\rho_{c,r}^m}}{PML_{c,r} * \delta_{w,c,r}^r} \right)^{\left( \frac{-1}{(\rho_{c,r}^m + 1)} \right)} \quad \forall c \in cmrl \quad (M12)$$

$$QT_{w,c,r} = \sum_{cp} (QMR_{w,cp,r} * margcor_{w,c,cp,r}) \quad \forall c \in ct2, r \in rgn \quad (M13)$$

The prices of the composite import commodities can also be expressed as a simple volume weighted averages of the of the import prices by region, (M5) where  $PM_{c,r}$  and  $QM_{c,r}$  are the price and quantity of the composite import commodity  $c$  by region  $r$ , and the weights are the volume shares of imports and are variable. Notice however that (M5) is only controlled by the set  $cm$ , in contrast to (X2) – the composite export price – which was also controlled by the set  $rgn$ , i.e., the region Globe was excluded. This reflects the fact that the region Globe does import commodities using the same trading assumption as other regions but only exports homogenous trade and transport services, which explains the need for the equation (X3).

The composite supply of the imported commodity ( $QM$ ) is a Leontief aggregate of imports with ‘small’ ( $QMS$ ) and ‘large’ ( $QML$ ) shares using appropriately defined input-output coefficients (M9 and M10). Similarly, the quantities imported of the ‘small’ share commodities by source region are defined by fixed (input-output) coefficients (M11). The use of a two stage Leontief nest in this case ensures no substitution possibilities between the aggregate imports  $QMS$  and  $QML$ ; if some substitution possibilities are required the nesting system used for production can be adapted.

The composite imports of commodities with ‘large’ shares are defined as CES aggregates of the imports from different regions ( $QMR$ ) (M12). The first order conditions come from the price definition terms for composite imports,  $PML$  (M1) and are only implemented for those cases where there were import transactions in the base period – this is controlled by the set  $cmr$ . Initially the formulation of M12 is not intuitive but, as demonstrated in Appendix A1, the formulation is a straightforward manipulation of a more conventional representation; this form, which is effectively a set of first-order conditions, is used because it reduces the number of equations in the model.

The composite (consumption) commodities are then a mixture of composite imports ( $QM$ ) and domestic demand from domestic production ( $QD$ ). The mixtures between the domestic and import supplies are determined by the substitution functions, Constant Elasticity of Substitution (CES) functions, (M6) with the optimal combinations of  $QM$  and  $QD$  being determined by first-order conditions, (M7). But, some commodities are non-traded and therefore M6 and M7 are implemented only if the commodity is traded, which leaves  $QQ$  undefined for non-traded commodities. By definition if there are no imports the quantity demanded by the domestic market is the amount produced, and if there is no domestic production the amount demanded is the amount imported. These two sets of possibilities are both covered by M8.

Also associated with any imported commodity is a specific quantity of trade and transport services. These services are assumed to be required in fixed quantities per unit of import by a specific region from another specific region, (M13) where the  $margcor$  are the trade and transport coefficients associated with a unit (quantity) import by region  $r$  from region  $w$ . This is only implemented for trade and transport commodities ( $ct2$ ) and for regions that ‘actually’ import goods ( $rgn$ ).

### 4.2.3 Commodity Price Block Equations

The composite price equations (CP1, CP2 and CP3) are derived from the first order conditions for tangencies to consumption and production possibility frontiers. By exploiting Euler's theorem for linearly homogeneous functions the composite prices can be expressed as expenditure identities rather than dual price equations for export transformation and import aggregation, such that  $PQS_{c,r}$  is the weighted average of the producer price of a commodity, when  $PD_{c,r}$  is the producer price of domestically produced commodities and  $PM_{c,r}$  the domestic price of the composite imported commodity, (CP1) where  $QD_{c,r}$  the quantity of the domestic commodity demanded by domestic consumers,  $QM_{c,r}$  the quantity of composite imports and  $QQ_{c,r}$  the quantity of the composite commodity. Notice how the commodity quantities are the weights. This composite commodity price (CP1) does not include sales taxes, which create price wedges between the purchaser price of a commodity ( $PQD_{c,r}$ ) and the producer prices ( $PQS_{c,r}$ ). Hence the purchaser price is defined as the producer price plus the sales taxes (CP2). This formulation means that the sales taxes are levied on all sales on the domestic market, irrespective of the origin of the commodity concerned.

#### **Commodity Price Block Equations**

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$$PQS_{c,r} = \frac{(PD_{c,r} * QD_{c,r}) + (PM_{c,r} * QM_{c,r})}{QQ_{c,r}} \quad \forall c \in (cd \cup cm), r \in rgn \quad (CP1)$$

$$PQD_{c,r} = PQS_{c,r} * (1 + TS_{c,r}) \quad \forall c \in (cd \cup cm), r \in rgn \quad (CP2)$$

$$PQCD_{c,r} = PQD_{c,r} * (1 + TV_{c,r}) \quad \forall c \in (cd \cup cm), r \in rgn \quad (CP3)$$

$$PXC_{c,r} = \frac{(PD_{c,r} * QD_{c,r}) + (PE_{c \in ce, r} * QE_{c \in ce, r})}{QXC_{c,r}} \quad (CP4)$$

$$\forall c \in cx, r \in rgn$$


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However, the model also includes Value Added Taxes ( $TV_{c,r}$ ) that are only levied on final demand by households. These are modelled as an *ad valorem* mark-up on the purchaser prices ( $PQCD_{c,r}$ ) paid by all domestic sources of demand in the economy (CP3).

The composite output price for a commodity,  $PXC_{c,r}$ , is also derived by exploiting Euler's theorem for linearly homogeneous functions, and is given by (CP4) where  $PD_{c,r}$  is the domestic producer price for the output of commodities supplied to the domestic market,  $QD_{c,r}$  is the supply of output to the domestic market,  $QE_{c,r}$  is the quantity exported by activities, and  $QXC_{c,r}$  is the quantity of domestic production by commodity.

#### 4.2.4 Numéraire Price Block

It is necessary to define a price numéraire for each region; for this model two alternative numéraire are defined so as to allow the modeller some discretion as to the choice of numéraire.<sup>15</sup> The consumer price indices ( $CPI_r$ ) are defined as base weighted sum of the commodity prices, where the weights are the value shares of each commodity in final demand ( $vqcdsh_{c,r}$ ), (N1). An advantage of with using the CPI as the numéraire is that the transactions within a region are expressed in real terms without the need to adjust values for price changes.

While the domestic producer price indices ( $PPI_r$ ) are defined as the weighted sums of the commodity prices received by producers on the domestic market, where the weights are the value shares of each commodity supplied by domestic producers to the domestic market ( $vqdsh_{c,r}$ ), (N2). This provides a convenient alternative price normalisation term; if the exchange rate is also fixed it serves to fix the real exchange rate.

#### *Numéraire Price Block Equations*

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$$CPI_r = \sum_c vqcdsh_{c,r} * PQD_{c,r} \quad \forall r \in rgn \quad (N1)$$

$$PPI_r = \sum_c vqdsh_{c,r} * PD_{c,r} \quad \forall r \in rgn \quad (N2)$$

$$ERPI = \sum_{ref} vqesh_{ref} * ER_{ref} \quad (N3)$$


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The exchange rate numéraire (N3) is defined as an exchange rate index for the set  $ref$ , which allows the user to define the reference region/regions for the exchange rate. In an

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<sup>15</sup> The price index not used as the numéraire provides useful additional information when interpreting the results. Other choices of numéraire are available, e.g., indices of import prices, and may be appropriate in some instances.

earlier version of the model the exchange rate of a single region, e.g., the USA, an aggregate including the USA, the OECD, EU, etc., was fixed and served as the numéraire. This alternative is still available if the membership of *ref* is limited to a single region but experience suggests that model performance is improved by including several regions in *ref*; typically, this is a basket of regions containing the OECD members but other alternatives are possible.<sup>16</sup>

Fixed country trade balances must be seen as specified in “real” terms defined by the global numéraire. So, if the US exchange rate is fixed to one, the global numéraire is defined as US dollars, and all trade balances can be seen as “real” variables defined in terms of the value of US exports. If the weighted exchange rate for a group of regions is chosen as global numéraire, trade balances can be seen as “claims” against a weighted average of exports by the group of regions.

Notice how both the consumer and producer price indices are implemented only for those regions that have consumption and production activities. Hence the Globe does not have its own price indices; rather the price indices for Globe are those of the reference region(s) in the model.

#### 4.2.5 Production Block Equations

The output price by activity ( $PX_{a,r}$ ) is defined by the shares of commodity outputs produced by each activity, (P1.1) where, for this case, the weights ( $ioqxcqx_{a,c,r}$ ) are equal to one where the commodities and activities match and zero otherwise, i.e., there is a one to one mapping between the commodity and activity accounts. The weights are derived from the information in the supply or make matrix.<sup>17</sup>

The value of output by activity is defined as the activity price ( $PX_{a,r}$ ) less production taxes ( $TX_{a,r}$ ) times the volume of output ( $QX_{a,r}$ ). This revenue must be divided between payments to primary inputs – the price of value added ( $PVA_{a,r}$ ) times the quantity of value added ( $QVA_{a,r}$ ) – and intermediate inputs – the price of aggregate intermediate inputs ( $PINT_{a,r}$ ) times the volume of aggregate intermediate inputs ( $QINT_{a,r}$ ) (P1.2). Given the

<sup>16</sup> A guiding principle for selecting the membership of *ref* is to choose a region or group of regions that accounts for a large share of global trade and output.

<sup>17</sup> When using GTAP data,  $ioqxcqx_{a,c,r}$  is always a diagonal matrix. However, using this specification for the activity price (PX) makes it easier to extend the model to include activities that produce multiple commodities and commodities that are produced by more than one activity.

assumption that intermediate inputs are used in fixed (volume) proportions, the price of aggregate intermediate inputs ( $PINT_{a,r}$ ) is defined as the weighted average price of the intermediate inputs where the weights are the (normalised) input-output coefficients (P1.3).

The default top level production function (P1.5), is a CES aggregation of aggregate primary and intermediate inputs, where the first order conditions for profit maximization (P1.6) determine the optimal ratio of the inputs. The efficiency factor ( $ADX_{a,r}$ ) and the factor shares parameters ( $\delta_{a,r}^x$ ) are calibrated from the data and the elasticities of substitution, from which the substitution parameters are derived ( $\rho_{a,r}^x$ ), are exogenously imposed. Note in this case the efficiency factor is declared as variable and is determined by (P1.4), where  $adxb_{a,r}$  is the vector of efficiency factors in the base solution,  $dabadx_{a,r}$  is a vector of absolute changes in the vector of efficiency factors,  $ADXADJ_r$  is a variable whose initial value is ONE,  $DADX_r$  is a variable whose initial value is ZERO and  $adx01_c$  is a vector of zeros and non zeros.<sup>18</sup> In the base solution the values of  $adx0_{a,r}$  and  $dabadx_{a,r}$  are all ZERO and  $ADXADJ_r$  and  $DADX_r$  are fixed as their initial values – a closure rule decision – then the applied efficiency factors are those from the base solution. This formulation allows flexibility in the formulation of the efficiency parameter that is especially useful in the contexts of a dynamic model or simulations that examine the implications of productivity growth or evaluate the productivity growth equivalent some policy change. The structure of this equation (P1.4) is identical to that used for the tax rate equations; a description of how these equations operate is provided when describing the tax rate equations (see below).

The production function (P1.5) is only implemented for members of the set  $aqx$ ; for its complement,  $aqxn$ , the CES function is replaced by Leontief functions. The Leontief functions require that aggregate intermediate inputs (P1.7) and aggregate values added (P1.8) are fixed proportions of the volumes of output. If there are no intermediate inputs used by an activity the top level function is automatically Leontief. In the default settings the Leontief assumption is also imposed automatically if the costs of total intermediate inputs accounts for 10 percent or less of total inputs; the user can change the share below which the Leontief assumption is imposed, by activity and region, when calibrating the model.

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<sup>18</sup> Typically, the values are either one or zero, i.e., the adjustment factor is switched on or off. Non zero values other than one switch on the adjustment factor and allow a more complex set of adjustments although it is important to be careful about the rationale for such a set of adjustments.

**Production Block Equations – Top Level**

$$PX_{a,r} = \sum_c ioqxcqx_{a,c,r} * PXC_{c,r} \quad \forall r \in rgn \quad (P1.1)$$

$$PX_{a,r} * (1 - TX_{a,r}) * QX_{a,r} = (PVA_{a,r} * QVA_{a,r}) + (PINT_{a,r} * QINT_{a,r}) \quad \forall r \in rgn \quad (P1.2)$$

$$PINT_{a,r} = \sum_c ioqint_{c,a,r} * PQD_{c,r} \quad \forall r \in rgn \quad (P1.3)$$

$$ADX_{a,r} = ((adxb_{a,r} + dabadx_{a,r}) * ADXADJ_r) + (DADX_r * adx01_{a,r}) \quad (P1.4)$$

$$QX_{a,r} = ADX_{a,r} * \left[ \delta_{a,r}^x * (QVA_{a,r})^{-\rho_{a,r}^x} + (1 - \delta_{a,r}^x) * (QINT_{a,r})^{-\rho_{a,r}^x} \right]^{1/\rho_{a,r}^x} \quad \forall r \in rgn, a \in aqx \quad (P1.5)$$

$$QVA_{a,r} = QINT_{a,r} * \left( \left( \frac{PINT_{a,r}}{PVA_{a,r}} \right) * \left( \frac{\delta_{a,r}^x}{(1 - \delta_{a,r}^x)} \right) \right)^{\left( \frac{1}{(1 + \rho_{a,r}^x)} \right)} \quad \forall r \in rgn, a \in aqx \quad (P1.6)$$

$$QINT_{a,r} = \sum_a ioqintqx_{a,r} * QX_{a,r} \quad \forall r \in rgn, a \in aqxn \quad (P1.7)$$

$$QVA_{a,r} = \sum_a ioqvaqx_{a,r} * QX_{a,r} \quad \forall r \in rgn, a \in aqxn \quad (P1.8)$$

$$QXC_{c,r} = \sum_a ioqxcqx_{a,c,r} * QX_{a,r} \quad \forall r \in rgn \quad (P1.9)$$

Finally, it is necessary to define the relationship between activity and commodity outputs, which is the counterpart to the price equation linking commodity and activity prices (P1.1). This is defined as a simple linear relationship whereby the commodity output is defined as the sum of the quantities of each commodity produced by each activity, (P1.9). But given the standard GTAP data, whereby each activity only produces a single commodity and *ioqxqxc* is an identity matrix, (P1.9) simply maps activities to commodities and *vice versa*.

**Production Block Equations – Second Level**

$$ADVA_{a,r} = \left( (advab_{a,r} + dabadva_{a,r}) * ADVAADJ_r \right) + (DADVA_r * adva01_{a,r}) \quad (P2.1)$$

$$ADFD_{f,a,r} = \left( (adfdb_{f,a,r} + dabadfd_{f,a,r}) * ADFDfADJ_f * ADFDaADJ_a * ADFDrADJ_r \right) \quad (P2.2)$$

$$QVA_{a,r} = ADVA_{a,r} * \left( \sum_{f2} \delta_{f2,a,r}^{va} * (ADFD_{f,a,r} * FD_{f2,a,r})^{-\rho_{a,r}^{va}} \right)^{\left( \frac{-1}{\rho_{a,r}^{va}} \right)} \quad (P2.3)$$

$\forall r \in rgn$

$$QVA_a = AD_a^{va} * \left[ \sum_{ff \in [map\_va\_f_{ff,a}f \text{ and } \delta_{ff,a}^{va}]} \delta_{ff,a}^{va} * ADFD_{ff,a} * FD_{ff,a}^{-\rho_a^{va}} \right]^{-\frac{1}{\rho_a^{va}}} \quad \forall \rho_a^{va} \quad (P3.9)$$

$$WF_{ff,r} * WFDIST_{ff,a,r} * (1 + TF_{ff,a,r})$$

$$= PVA_{a,r} * QVA_{a,r} * \left[ \sum_{ff} \delta_{ff,a,r}^{va} * (ADFD_{ff,a,r} * FD_{ff,a,r})^{-\rho_{a,r}^{va}} \right]^{(-1)} \quad (P2.4)$$

$$* \delta_{ff,a,r}^{va} * (ADFD_{ff,a,r})^{-\rho_{a,r}^{va}} * (FD_{ff,a,r})^{(-\rho_{a,r}^{va}-1)}$$

$\forall r \in rgn, ff \in f, \delta_{ff,a,r}^{va} > 0$

$$WF_f * WFDIST_{ff,a} * (1 + TF_{ff,a})$$

$$= PVA_a * AD_a^{va} * \left[ \sum_{ff \in \delta_{ff,a}^{va}} \delta_{ff,a}^{va} * ADFD_{ff,a} * FD_{ff,a}^{-\rho_a^{va}} \right]^{\left( \frac{1+\rho_a^{va}}{\rho_a^{va}} \right)} * \delta_{ff,a}^{va} * FD_{ff,a}^{(-\rho_a^{va}-1)}$$

$$= PVA_a * QVA_a * AD_a^{va} * \left[ \sum_{ff \in \delta_{ff,a}^{va}} \delta_{ff,a}^{va} * ADFD_{ff,a} * FD_{ff,a}^{-\rho_a^{va}} \right]^{-1}$$

$$* \delta_{ff,a}^{va} * ADFD_{ff,a}^{-\rho_a^{va}} * \delta_{ff,a}^{va} * FD_{ff,a}^{(-\rho_a^{va}-1)} \quad \forall \delta_{f,a}^{va} \text{ and } map\_va\_ff_{ff,a} \quad (P3.10)$$

$$QINTD_{c,r} = \sum_a ioqint_{c,a,r} * QINT_{a,r} \quad \forall r \in rgn, cintd_{c,r} \quad (P2.4)$$

The second and third level production functions use factors of production ( $FD$ ) that are defined over the set  $ff$  of which the natural factors, set  $f$ , are a subset and the other members of  $ff$  are aggregate factors.<sup>19</sup> Given the structure of the GTAP database<sup>20</sup> this variant of the ANARRES model is specified so that the only aggregate factor is (aggregate) labour, which is defined at the third level, while the second level defines the production function for value added ( $QVA$ ) that uses aggregate labour and all the non-labour natural factors of production. The second level production functions are CES aggregation functions over the natural and aggregate factors that are demanded by each activity ( $FD_{f2,a,r}$ ), with efficiency factors ( $ADVA_{a,r}$ ) and the factor shares ( $\delta_{f,a,r}^{va}$ ) calibrated from the data and the elasticities of substitution, from which the substitution parameters are derived ( $\rho_{a,r}^{va}$ ), are exogenously imposed (P2.3). Note how the production function for  $QVA$  is specified to use the subset  $f2(ff)$  of factors; this set includes (aggregate) labour and all the non-labour natural factors. The associated first-order conditions for optimal factor combinations are derived from equalities between the wage rates for each factor in each activity and the values of the marginal products of those factors in each activity, (P2.4); while defined over  $ff$  its operation is limited to  $f2$ . The actual wage rate for a specific factor used by a specific activity is defined as the average wage rate for that factor ( $WF_{ff,r}$ ) times a factor and activity specific factor ‘efficiency’ parameter ( $WFDIST_{ff,a,r}$ ); these ratios of payments to factor  $ff$  from activity  $a$  are included to allow for non-homogenous factors where the differentiation is defined solely in terms of the activity that employs the factor. However the actual returns to a factor must be adjusted to allow for taxes on factor use ( $TF_{ff,a,r}$ ).

<sup>19</sup> Since only natural factors,  $f$ , receive actual income the use of the set  $ff$  in the production modules allows the set  $f$  the control the distribution of factor incomes. Similarly, it should be noted that only natural factors should be subjected to factor use taxes ( $TF$ ).

<sup>20</sup> In the GTAP database there are five natural factors; skilled and unskilled labour, capital, land and natural resources. In the fully disaggregated database skilled and unskilled labour and capital are not differentiated across activities while land and natural resources are segmented, i.e., no activity employs both land and natural resources. For the ANARRES model it is recommended that natural factors are not aggregated and in particular that land and natural resources are NEVER aggregated AND that aggregates are not formed across activities that use land and natural resources in the disaggregated data.

The efficiency factors are declared as variables (P2.1), where  $advab_{a,r}$  is the vector of efficiency factors in the base solution,  $dabadva_{a,r}$  is a vector of absolute changes in the vector of efficiency factors,  $ADVAADJ_r$  is a variable whose initial value is ONE,  $DADVA_r$  is a variable whose initial value is ZERO and  $adva01_{a,r}$  is a vector of zeros and non-zeros.<sup>21</sup> In the base solution the values of  $advab_{a,r}$  and  $dabadva_{a,r}$  are all ZERO and  $ADVAADJ_r$  and  $DADVA_r$  are fixed as their initial values – a closure rule decision – then the applied efficiency factors are those from the base solution. A similar specification is adopted for factor specific efficiency factors, i.e., factor that can alter/adjust the stock-flow relationship between factor quantities and factor services, although it differs in the adjustment mechanism (P2.2). Specifically, only a multiplicative variant is defined and then three adjustment variables are defined that allow for factor specific ( $ADFDfADJ_f$ ), activity specific ( $ADFDaADJ_a$ ) and region specific ( $ADFDrADJ_r$ ) adjustments.

Since production uses intermediate inputs, it is also necessary to specify the demand for intermediate inputs ( $QINTD_{c,r}$ ). This is done from the perspective of commodity demands, i.e., it is summed over activities to produce the demand for intermediate inputs by commodity rather than by activity (P2.4).

The third level production functions (P3.1) define the quantities of aggregate factors ( $fag$ ) as CES aggregates of the labour factors ( $l$ ). As elsewhere the efficiency factors ( $ADFAG_{fag,a,r}$ ) and the factor shares ( $\delta_{fag,l,a,r}^{fd}$ ) calibrated from the data and the elasticities of substitution, from which the substitution parameters are derived ( $\rho_{fag,a,r}^{fd}$ ), are exogenously imposed. The matching first order conditions (P3.2) define the wage rate for a specific factor used by a specific activity as the average wage rate for that factor ( $WF_{l,r}$ ) times a factor and activity specific factor ‘efficiency’ parameter ( $WFDIST_{l,a,r}$ ); these ratios of payments to factor  $l$  from activity  $a$  are included to allow for non-homogenous factors where the differentiation is defined solely in terms of the activity that employs the factor. However the actual returns to a factor must be adjusted to allow for taxes on factor use ( $TF_{l,a,r}$ )

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<sup>21</sup> Typically, the values are either one or zero, i.e., the adjustment factor is switched on or off. Nonzero values other than one switch on the adjustment factor and allow a more complex set of adjustments although it is important to be careful about the rationale for such a set of adjustments.

**Production Block Equations – Third Level**

$$FD_{ff,a,r} = ADFAG_{ff,a,r} * \left( \sum_l \delta_{ff,l,a,r}^{fd} * (FD_{l,a,r})^{\rho_{ff,a,r}^{fd}} \right)^{\left( \frac{-1}{\rho_{ff,a,r}^{fd}} \right)} \quad (P3.1)$$

$\forall r \in rgn, \delta_{ff,l,a,r}^{fd}, ff \in fag$

$$\begin{aligned} &WF_{l,r} * WFDIST_{l,a,r} * (1 + TF_{l,a,r}) \\ &= WF_{ff,r} * WFDIST_{ff,a,r} * (1 + TF_{ff,a,r}) * FD_{ff,a,r} \\ &* \left[ \sum_l \delta_{ff,l,a,r}^{fd} * FD_{l,a,r}^{-\rho_{ff,a,r}^{fd}} \right]^{(-1)} * \delta_{ff,l,a,r}^{fd} * FD_{l,a,r}^{(-\rho_{ff,a,r}^{fd}-1)} \end{aligned} \quad (P3.2)$$

$\forall r \in rgn, \delta_{ff,l,a,r}^{fd}, ff \in fag$

$$ADFAG_{ff,a} = (adfabg_{ff,a} + dabfabg_{ff,a}) + (ADFAGfADJ_{ff} * ADFAGaADJ_a) \quad (P3.12)$$

$$FD_{ff,a} = ADFAG_{ff,a} * \left( \sum_{\substack{ffp \in [\delta_{ff,ffp,a}^{fd} \\ \text{and } map\_fagg\_f]}} \delta_{ff,ffp,a}^{fd} * (FD_{ffp,a})^{\rho_{ff,a}^{fd}} \right)^{\left( \frac{-1}{\rho_{ff,a}^{fd}} \right)}$$

$\forall \sum_{ffp} map\_fagg\_ff_{ff,ffp,a}$

(P3.13)

$$\begin{aligned} &WFA_{ffp,a} * (1 + TF_{ffp,a}) \\ &= WFA_{ff,a} * (1 + TF_{ff,a}) * FD_{ff,a} \\ &* \left[ \sum_{\substack{ffpp \in [\delta_{ff,ffpp,a}^{fd} \\ \text{and } map\_fagg\_ff]}} \delta_{ff,ffpp,a}^{fd} * FD_{ffpp,a}^{-\rho_{ff,a}^{fd}} \right]^{(-1)} * \delta_{ff,ffpp,a}^{fd} * FD_{ffpp,a}^{(-\rho_{ff,a}^{fd}-1)} \end{aligned}$$

$\forall \delta_{ff,ffpp,a}^{fd}, map\_fagg\_ff_{ff,ffpp,a}$

(P3.14)

**4.2.6 Factor Block Equations**

The total income received by each factor account ( $YF_f$ ) is defined as the summation of the earnings of that factor across all activities (F1).<sup>22</sup> However, only a proportion of total factor income is available for distribution to the domestic institutional accounts ( $YFDIST_{f,r}$ ). First, allowance must be made for depreciation, which it is assumed takes place at fixed rates

<sup>22</sup> Note that only natural factors,  $f$ , receive actual income.

( $deprec_{f,r}$ ) relative to factor incomes, and then second, allowance must be made for the payment of factor income taxes ( $TYF_{f,r}$ )<sup>23</sup> (F2).

### **Factor Block Equations**

$$YF_{f,r} = \sum_a WF_{f,r} * WFDIST_{f,a,r} * FD_{f,a,r} \quad \forall r \in rgn \quad (F1)$$

$$YFDIST_{f,r} = \left( YF_{f,r} - (deprec_{f,r} * YF_{f,r}) \right) * (1 - TYF_{f,r}) \quad \forall r \in rgn \quad (F2)$$

#### 4.2.7 Household Block Equations

Households acquire income from only one source in this model; the sale of factor services. Therefore household income ( $YH_{h,r}$ ) is defined simply as the sum of factor incomes available for distribution. In this variant allowance is made for the possibility of multiple households by indexing households on the set  $h$  and including a set of distribution parameters ( $hvas_{h,f,r}$ ) that are defined as the shares of each factor demanded in the economy that is supplied by each household. If the model is to be calibrated for multiple households, the user needs to augment the database. In the ‘standard’ case of one household all the shares equal one.

Household consumption demand is derived in two stages. In the first stage (H2) household consumption expenditures ( $HEXP_{h,r}$ ) are defined as household incomes after the payment of direct taxes and savings and inter household transfers. Note how the saving rates are defined as proportions of after tax incomes that are saved; this is important for the calibration of the income tax and savings parameters.

The household utility functions are assumed to be Stone-Geary, i.e., a linear expenditure system, which means that household consumption demand consists of two components, ‘subsistence’ demand ( $qcdconst_{c,h,r}$ ) and ‘discretionary’ demand, and the equation must

<sup>23</sup> In the GTAP database direct taxes paid by domestic institutions, households, NPISH and incorporated business enterprises, usually known as enterprises, are recorded as direct taxes paid by factors (see the GTAP database documentation for the details). In the ANARRES database these direct taxes are assigned to the household account; thus the implicit assumption is that the household account encompasses households, NPISH and enterprises. The tax on factor incomes is however kept as an instrument because some direct taxes are levied on factors, e.g., social security contributions.

therefore capture both elements. Discretionary demand is defined as the marginal budget shares ( $\beta$ ) spent on each commodity out of ‘uncommitted’ income, i.e., household consumption expenditure less total expenditure on ‘subsistence’ demand. The quantities of each commodity demanded by the household are then defined by the shares of household consumption expenditure. The Stone-Geary function collapses to a Cobb-Douglas utility function if all the income elasticities of demand are set equal to one and the Frisch parameter, the elasticity of the marginal utility of income, is also set to one. One advantage of the Cobb-Douglas specification is that it results in the changes in the values for household consumption expenditures ( $HEXP_{h,r}$ ) being equal to the changes in an equivalent variation measure of household welfare.

### ***Household Block Equations***

$$YH_{h,r} = \sum_f hvash_{h,f,r} * YFDIST_{f,r} \quad \forall r \in rgn \quad (H1)$$

$$HEXP_{h,r} = \left( YH_{h,r} * (1 - TYH_{h,r}) \right) * (1 - SHH_{h,r}) \quad \forall r \in rgn \quad (H2)$$

$$\begin{aligned}
 QCD_{c,h,r} * PQCD_{c,r} &= \left( PQCD_{c,r} * qcdconst_{c,h,r} \right) \\
 &+ \beta_{c,h,r} * \left( HEXP_{h,r} - \sum_c PQCD_{c,r} * qcdconst_{c,h,r} \right) \quad (H3) \\
 &\quad \forall r \in rgn
 \end{aligned}$$

Note how the prices for final demand commodities are specified as inclusive of *ad valorem* value added taxes (*TV*). This VAT is specified as additional to other ‘general’ sales taxes (*TS*) levied on domestic demand; as such it is a simplification because it does not allow for differential realised rates of rebate of VAT on intermediate input demand – the implicit presumption is that the rebate rates are equal to 100 percent or that the rebate rate does not change in any simulation. While this is a strong assumption the increasing importance of VAT systems means that ignoring the VAT issue is arguably unwise; moreover, it is recommended in the GLOBE model that the GST rates (*TS*) are NOT used as a tax replacement instrument and that they are not changed in experiments.<sup>24</sup>

<sup>24</sup> *De facto* this advice means that sales taxes rates should be treated as an unchanging distortion in the underlying data and simulations are conducted under the implicit assumption that the degree of distortion

#### 4.2.8 Government Tax Block Equations

There are nine tax instruments. Eight are defined as simple *ad valorem* rates dependent upon the values of imports, exports, sales, household demand, production and factor use by activities and the levels of factor and household and income. In this version of the model one of the tax rates is defined by reference to the quantity of imports - a specific tax rate – but other tax rates could easily be expressed using bases other than values.

All tax rates are variables in this model and for each tax instrument a series of factors are declared to facilitate policy experiments. The tax rates in the base solution are defined as parameters, e.g.,  $tmb_{w,c,r}$  are the import tariff rates by commodity  $c$  imported from region  $w$  in region  $r$  in the base solution, and the tax rate equations then allow for varying the tax rates in four different ways. Two of the methods use variables that can be solved for optimum values in the model according to the choice of closure rule and two methods allow for deterministic adjustments to the structure of the tax rates. The operations of these methods are discussed in detail only for the equations for import duties while the other equations are simply reported.

In the import tariff rate equation (T1.1)  $tmb_{w,c,r}$  is the vector of import duties in the base solution,  $dabtm_{w,c,r}$  is a vector of absolute changes in the vector of import duties taxes,  $TMADJ_r$  is a region specific variable whose initial value is ONE,  $DTM_r$  is a region specific variable whose initial value is ZERO and  $tm01_{w,c,r}$  is a vector of zeros and non-zeros. In the base solution the values of  $tm01_{w,c,r}$  and  $dabtm_{w,c,r}$  are all ZERO and  $TMADJ_r$  and  $DTM_r$  are fixed as their initial values – this is a closure rule decision. Given this decision the model treats the tax rates as (fixed) parameters and the applied import tariffs are those from the base solution. The different methods of adjustment can be considered in turn.

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is unchanged. With respect to intermediate inputs this is not an issue in most model situations since the Leontief assumption makes the composition of intermediate inputs invariant to price changes. The energy variant of the ANARRES model relaxes this assumption because energy input uses are made price sensitive AND because GTAP has collected and provided enhanced data for sales taxes on energy.

### Government Tax Rates Equations

$$TM_{w,c,r} = \left( (tmb_{w,c,r} + dabtm_{w,c,r}) * TMADJ_r \right) + (DTM_r * tm01_{w,c,r}) \quad \forall c \in cmr \quad (T1.1)$$

$$TE_{c,w,r} = \left( (teb_{c,w,r} + dabte_{c,w,r}) * TEADJ_r \right) + (DTE_r * te01_{c,w,r}) \quad \forall c \in cer \quad (T1.2)$$

$$TS_{c,r} = \left( (tsb_{c,r} + dabts_{c,r}) * TSADJ_r \right) + (DTS_r * ts01_{c,r}) \quad (T1.3)$$

$$\forall r \in rgn, c \in (cd \cup cm)$$

$$TV_{c,r} = \left( (tvb_{c,r} + dabtv_{c,r}) * TVADJ_r \right) + (DTV_r * tv01_{c,r}) \quad (T1.4)$$

$$\forall r \in rgn, c \in (cd \cup cm)$$

$$TX_{a,r} = \left( (txb_{a,r} + dabtx_{a,r}) * TXADJ_r \right) + (DTX_r * tx01_{a,r}) \quad \forall r \in rgn \quad (T1.5)$$

$$TYF_{f,r} = \left( (tyfb_{f,r} + dabtyf_{f,r}) * TYFADJ_r \right) + (DTYF_r * tyf01_{f,r}) \quad \forall r \in rgn \quad (T1.6)$$

$$TYH_{h,r} = \left( (tyhb_{h,r} + dabtyh_{h,r}) * TYHADJ_r \right) + (DTYH_r * tyh01_{h,r}) \quad \forall r \in rgn \quad (T1.7)$$

$$TF_{f,a,r} = \left( (tbf_{f,a,r} + dabtf_{f,a,r}) * TFADJ_r \right) + (DTF_r * ty01_{f,a,r}) \quad \forall r \in rgn \quad (T1.8)$$

1. If  $TMADJ_r$  for one region is made a variable, which requires the fixing of another variable for that region, and all other initial conditions hold then the solution value for  $TMADJ_r$  yields the optimum equiproportionate change in the import duty rates necessary to satisfy model constraints, e.g., if  $TMADJ_r$  equals 1.1 then all applied (non-zero) import duty rates (that are found in the base data) for the specified region are increased by 10%.
2. If any element of  $dabtm_{w,c,r}$  is not zero, and all the other initial conditions hold, then an absolute change in the initial import tariff rate for the relevant commodity is imposed, e.g., if  $tmb_{w,c,r}$  for one element of  $c$  is 0.1 (a 10% import duty) and  $dabtm_{w,c,r}$  for that element is 0.05, then the *applied* import tariff rate is 0.15 (15%).
3. If  $TMADJ_r$  for one region is made a variable, which requires the fixing of another variable for that region, any elements of  $dabtm_{w,c,r}$  are non zero and all

other initial conditions hold, then the solution value for  $TMADJ_r$  yields the optimum equiproportionate change in the *applied* import duty rates, i.e.,  $tmb_{w,c,r} + dabtm_{w,c,r}$  (and these applied rates can be different from those in the base in which  $dabtm_{w,c,r}$  is set at zero).

4. If  $DTM_r$  for one region is made a variable, which requires the fixing of another variable for that region, AND at least one element of  $tm01_{w,c,r}$  is ONE then the subset of elements of  $tm0_{w,c,r}$  identified by  $tm01_{w,c,r}$  are allowed to (additively) increase by an equal absolute amount determined by the solution value for  $DTM_r$  and the initial values of the import duty rates, e.g., if food products are to be excluded from the change in tax rates then the elements of  $tm01_{w,c,r}$  corresponding to the food commodities are (left as) zeros. Note how in this case it is necessary to both ‘free’ a variable and give values to a parameter for a solution to emerge. If the change in the applied tax rates is to be other than equal absolute values then values of  $tm01_{w,c,r}$  other than one can be applied, e.g., if the changes in the import duties on food products are to be half those on other sectors then the elements of  $tm01_{w,c,r}$  corresponding to the food commodities can be set to 0.5 and for the other commodities can be set to 1.

This combination of alternative adjustment methods covers the range of common tax rate adjustments used in the majority of applied applications while being flexible and easy to use. However, experience has shown that when working with GTAP data it is very important to check the tax rates that are applied in the base solution; in some aggregations some of the applied tax rates only differ marginally from zero but are a mix of negatives and positives, in such cases it may be necessary to exogenously reset the tax rates to avoid apparently odd results. All the model parameters are exported to a GDX file and can be easily accessed using GDXViewer and/or SeeResults.<sup>25</sup>

The other tax rate equations follow the same structure: export taxes ( $TE_{c,r}$ ) are defined in (T1.2), sales taxes ( $TS_{c,r}$ ) are defined in (T1.3), VAT ( $TV_{c,r}$ ) rates are defined in (T1.4), production tax rates ( $TX_{a,r}$ ) are defined in (T1.5), factor income tax rates ( $TYF_{f,r}$ ) are defined in (T1.6), household income rates ( $TYH_{h,r}$ ) are defined in (T1.7) and factor use tax rates ( $TF_{f,r}$ ) are defined in (T1.8).

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<sup>25</sup> See Section 6 on complementary programmes.

**Government Tax Revenues Equations**

$$MTAX_r = \sum_w \sum_c (TM_{w,c,r} * PWM_{w,c,r} * ER_r * QMR_{w,c,r}) \quad \forall r \in rgn \quad (T2.1)$$

$$ETAX_r = \sum_w \sum_c (TE_{c,w,r} * PWE_{c,w,r} * ER_r * QER_{c,w,r}) \quad \forall r \in rgn \quad (T2.2)$$

$$STAX_r = \sum_c \left( TS_{c,r} * POS_{c,r} * \left( QINTD_{c,r} + \sum_h QCD_{c,h,r} + QGD_{c,r} + QINVD_{c,r} \right) \right) \quad \forall r \in rgn \quad (T2.3)$$

$$VTAX_r = \sum_c \sum_h (TV_{c,r} * PQD_{c,r} * QCD_{c,h,r}) \quad \forall r \in rgn \quad (T2.4)$$

$$ITAX_r = \sum_a (TX_{a,r} * PX_{a,r} * QX_{a,r}) \quad \forall r \in rgn \quad (T2.5)$$

$$FYTAX_r = \sum_f (TYF_{f,r} * (YF_{f,r} - (deprec_{f,r} * YF_{f,r}))) \quad \forall r \in rgn \quad (T2.6)$$

$$HTAX_r = \sum_h (TYH_{h,r} * YH_{h,r}) \quad \forall r \in rgn \quad (T2.7)$$

$$FTAX_r = \sum_f \sum_a (TF_{f,a,r} * WF_{f,r} * WFDIST_{f,a,r} * FD_{f,a,r}) \quad \forall r \in rgn \quad (T2.8)$$

The government tax revenue equations simply sum the revenues from each different tax instrument for each region. These are not strictly necessary for the model since the equations could be collapsed into a single government income equation (see G1 below). However it is useful to carry around these additional variables since they can then be used in model closures to accommodate specific government tax revenue objectives and they are useful sources of information when analysing simulation results.<sup>26</sup> *Ad valorem* Import duty revenues ( $MTAX_r$ ) are defined as total *ad valorem* import duty revenue in region  $r$  (T2.1); Export tax revenues ( $ETAX_r$ ) are defined as total export tax revenue in region  $r$  (T2.2); sales tax revenues ( $STAX_r$ ) are defined as total sales tax revenue in region  $r$  (T2.3); VAT revenues ( $VTAX_r$ ) are defined as total VAT revenue in region  $r$  (T2.4); production tax revenues ( $ITAX_r$ ) are defined as total

<sup>26</sup> It is a simple matter to generate such aggregates from model results as part of the reported output of the simulations. The trade-off between the increase in model ‘size’ associated with extra variables and reduction in the size of the files that generate results is a matter of judgement; the general approach used here is to include as variable such aggregates that may have substantive benefits in terms of transparency and simulation formulation.

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production tax revenue in region  $r$  (T2.5); factor income tax revenues ( $FYTAX_r$ ) are defined as total factor income tax revenue in region  $r$  (T2.6); household income tax revenues ( $HTAX_r$ ) are defined as total household income tax revenue in region  $r$  (T2.7) and factor use tax revenues ( $FTAX_r$ ) are defined as total factor use tax revenue in region  $r$  (T2.8).

#### 4.2.9 Government Block Equations

Government income ( $YG_r$ ) is defined as the sum of government tax revenues (G1), where the tax revenues are treated as expenditures by the accounts paying the taxes and hence are defined in the tax block. While this approach adds equations it has the arguable advantage of being more transparent and easier to modify. Note how there is no provision for government to receive incomes from non tax sources in this version; this reflects the fact that in the base GTAP database no such incomes are recorded.

#### ***Other Government Equations***

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$$YG_r = MTAX_r + ETAX_r + STAX_r + VTAX_r + ITAX_r + FYTAX_r + HTAX_r + FTAX_r \quad \forall r \in rgn \quad (G1)$$

$$QGD_{c,r} = qgdconst_{c,r} * QGDADJ_r \quad \forall r \in rgn \quad (G2)$$

$$EG_r = \sum_c PQD_{c,r} * QGD_{c,r} \quad \forall r \in rgn \quad (G3)$$


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Government demand for commodities (G2) is assumed fixed in real terms, i.e., the volume is fixed,<sup>27</sup> but can be scaled or allowed to vary using an adjustment factor ( $QGDADJ_r$ ). The precise specification depends upon the choice of closure rule (see below). Thereafter Government consumption expenditure ( $EG_r$ ) is defined as the sum of commodity consumption (G3). The advantage of separately expressing the volume and value of government expenditures is the increased flexibility it provides in the choice of closure rules for the government account. This arrangement allows adjustment of government demand either through the volume, or the expenditure or the value share of final demand (see below).

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<sup>27</sup> This assumption means that the implicit utility function for the governments has a Leontief form. Other options are possible – and easily implemented, e.g., Cobb-Douglas, CES, LES, etc., but the literature does not provide a clear theoretical rationale for identifying the appropriate form.

#### 4.2.10 Capital Account Block Equations

Income to the capital (savings and investment) account, total savings, comes from household savings, depreciation allowances, government savings ( $KAPGOV_r$ ) and the surplus on the capital account of the balance of payments ( $KAPWOR_r$ ), and hence is simply defined as the sum of savings by domestic and ‘foreign’ agents (K1.2).

In this model the household savings rates are declared as variables ( $SHH_{h,r}$ ) that define the proportions of income saved after the payment of income taxes. The savings rate equations (K1.1) used the same adjustment structure as used for the tax rate equations; hence  $shh0_{h,r}$  are the base solution savings rates  $dabshh_{h,r}$  are absolute changes in the base savings rates,  $SADJ_r$  are multiplicative adjustment factors,  $DSHH_r$  are additive adjustment factors and  $shh01_{h,r}$  is a matrix of zero and non-zero values that determine for which households and regions the savings rates can adjust additively. Note that household savings are taken out of after-tax income.

#### **Savings Block Equations**

$$SHH_{h,r} = \left( (shhb_{h,r} + dabshh_{h,r}) * SADJ_r \right) + (DSHH_r * shh01_{h,r}) \quad \forall r \in rgn \quad (K1.1)$$

$$TOTSAV_r = \left( \sum_h (YH_{h,r} * (1 - TYH_{h,r})) * (SHH_{h,r}) \right) + \sum_f deprec_{f,r} * YF_{f,r} + KAPGOV_r + (KAPWOR_r * ER_r) \quad \forall r \in rgn \quad (K1.2)$$

Government savings are calculated as residual (see the  $KAPGOV_r$  equations, MC3.1, below). The surplus on the capital account ( $KAPWOR_r$ ) is defined in terms of the foreign currency (see MC3.4 and MC3.3) and therefore the exchange rate appears in this equation (this is a matter of preference).

Investment demand is modeled in a similar way to government demand. Demand for commodities (K2.1) used in investment is assumed to be in fixed volume<sup>28</sup> ( $qinvdconst_{c,r}$ ) multiplied by an investment-scaling variable ( $IADJ_r$ ) that can accommodate changes in the exogenously determined level of investment and/or changes in the availability of funds for investment. The second stage (K2.2) captures the price effect by identifying the total value of investment ( $INVEST_r$ ). This arrangement allows adjustment of investment demand either through the volume, or the expenditure or the value share of final demand (see below).

### ***Investment Block Equations***

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$$QINVD_{c,r} = IADJ_r * qinvdconst_{c,r} \quad \forall r \in rgn \quad (K2.1)$$

$$INVEST_r = \sum_c (PQD_{c,r} * QINVD_{c,r}) \quad \forall r \in rgn \quad (K2.2)$$


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#### 4.2.11 Market Clearing Block Equations

In the base solution to the model the market clearing, or equilibrium, conditions are relatively straightforward. Factor supplies must equal factor demands plus any unemployed labour in a region (MC1). Thus the factor supplies cannot be simply equated to the sum of factor demands in the base period but must equal the sum of factor demand plus any unemployed factors. As such the default specification of the model is NOT full employment but rather that there is the possibility of unemployment.

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<sup>28</sup> This assumption means that the implicit utility function for the investment demand has a Leontief form; other options are possible – and easily implemented, e.g., Cobb-Douglas, CES, LES, etc. In fact, the composition of investment demand defines the ‘technology’ used to produce new capital goods.

**Factor Account Equation**

$$FS_{f,r} = \sum_a FD_{f,a,r} + UNEMP_{f,r} \quad \forall r \in rgn \quad (MC1.1)$$

$$UNEMP_{f,a} \geq 0 \quad \forall r \in rgn \quad (MC1.2)$$

The (composite) commodity supplies must equal (composite) commodity demands (MC2). It appears that there is no equilibrium condition for the supply of domestic output to the domestic market. In fact this is achieved through the commodity output equation (P1.9), which could have been treated as a market clearing equation.

**Commodity Account Equations**

$$QQ_{c,r} = QINTD_{c,r} + \sum_h QCD_{c,h,r} + QGD_{c,r} + QINVD_{c,r} \quad (MC2.1)$$

$$\forall c \in (cd \cup cm), r \in rgn$$

The commodity trade accounts define the market clearing conditions for bilateral trade. The *FOB* prices for imports ( $PWMFOB_{w,c,r}$ ) for all imports by destination and source must be equal to the *FOB* prices for exports ( $PWE_{c,w,r}$ ) by source and destination (MC3.1). In addition the quantities of imports ( $QMR_{w,c,r}$ ) for all imports by destination and source must be equal to the quantities of exports ( $QER_{c,w,r}$ ) by source and destination (MC3.2). These equations are not completely straightforward since it is necessary in their implementation to employ mappings between exporting and importing regions that require the ‘switching’ of labels on accounts within the equation.

### Commodity Trade Account Equations

$$\sum_w (P_{WM}_{w,c,r} * Q_{MR}_{w,c,r}) = \sum_w (P_{WE}_{c,w,r} * Q_{ER}_{c,w,r}) + GLOBESLACK$$

$$\forall c \in ct2, r \notin rgn$$

$$P_{WMFOB}_{w,c,r} = P_{WE}_{c,w,r} \quad \forall c \in cmr, map\_r\_w, map\_w\_r \quad (MC3.1)$$

$$Q_{MR}_{w,c,r} = Q_{ER}_{c,w,r} \quad \forall c \in cmr, map\_r\_w, map\_w\_r \quad (MC3.2)$$

The trade consistency equations do not however deal with the requirements for market clearing with respect to the trade transactions undertaken by the Globe region. However similar conditions apply for the margins trade. These require that the total demand for each and every trade and transport service ( $QT_{w,c,r}$ ) is exactly equal to the exports of that service by Globe ( $QER_{c,w,"glo"}$ ) and the import prices of margin services ( $PT_{c,r}$ ) must equal the export prices ( $FOB$ ) from Globe; these conditions are imposed by (MC4.1) and (MC4.2) respectively.

### Margin Trade Account Equations

$$\sum_w QT_{w,c,r} = \sum_w QER_{c,w,"glo"} \quad \forall c \in ct2, r \in rgn \quad (MC4.1)$$

$$PT_{c,r} = P_{WE}_{c,w,"glo"} \quad \forall c \in ct2, r \in rgn \quad (MC4.2)$$

#### 4.2.12 Macroeconomic Closure Block Equations

The government account is cleared by defining government savings ( $KAPGOV_r$ ) as the difference between government income and government expenditure on consumption and transfers; hence government savings are explicitly treated as a residual, (MC5.1). The deficit/surplus on the current account is computed in two-stages. First the bilateral trade balances ( $KAPREG_{w,r}$ ) are calculated as the difference in the values of imports and exports, for first the trade flows between regions other than Globe (MC5.2) and then for trade between Globe and all other regions (MC5.3) – the latter being the trade balances on margins trade. These transactions are valued in terms of the global numéraire. Then the overall balance of

trade ( $KAPWOR_r$ ) is computed for each region, (MC5.4). Finally, the commodity trade balance for Globe is defined (MC5.5), since this should be zero by definition a slack variable ( $GLOBESLACK$ ) is attached.

### *Investment and Savings Account Equations*

$$KAPGOV_r = YG_r - EG_r \quad \forall r \in rgn \quad (MC5.1)$$

$$KAPREG_{w,r} = \left( \sum_c PWMFOB_{w,c,r} * QMR_{w,c,r} \right) - \left( \sum_c PWE_{c,w,r} * QER_{c,w,r} \right) \quad (MC5.2)$$

$\forall w \in wgn$

$$KAPREG_{w,r} = \left( \sum_c \sum_w PT_{c,r} * QT_{w,c,r} \right) - \left( \sum_c PWE_{c,w,r} * QER_{c,w,r} \right) \quad (MC5.3)$$

$\forall w \notin wgn$

$$KAPWOR_r = \sum_w KAPREG_{w,r} \quad \forall r \quad (MC5.4)$$

$$(MC5.5)$$

The absorption closure equations exist to support closure rule choices relating to the distribution of final demand between the institutions within regions. The value of final demand by region ( $VFDOMD_r$ ) is simply the sum of the value of final demand across the three sources of final demand – households, government and investment (MC6.1). The value share of final demand accounted for by investment ( $INVESTSH_r$ ) is defined in (MC6.2), and the value share of final demand accounted for by government ( $VGDSH_r$ ) is defined in (MC6.3). No similar expression exists for the households because household expenditures are defined after taxes and savings and it is difficult to justify setting the household shares relative to the value of total final demand since this would nullify the distributional consequences of a policy shock. If the expenditure shares by investment and government are fixed then the expenditure share of ALL households will by definition be fixed and  $HEXP_r$  could be fixed for individual households if there was good reason.

**Absorption Closure Equations**

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$$VFDOMD_r = \sum_c \left( PQCD_{c,r} * \sum_h QCD_{c,h,r} \right) + \sum_c \left( PQD_{c,r} * (QGD_{c,r} + QINVD_{c,r}) \right) \quad (MC6.1)$$

$\forall r \in rgn$

$$INVESTSH_r * VFDOMD_r = INVEST_r \quad \forall r \in rgn \quad (MC6.2)$$


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4.2.14 Slacks Block Equations

The final equations are for slacks. The satisfaction of Walras’s law requires that if all other accounts balance then so must the final account; thus the difference between savings and investment for all regions that save should always be zero and hence the variable *WALRAS<sub>r</sub>* should equal zero in (M87.1). That this variable equals zero is a good check on the correct specification of the model. Finally, the global trade balance must by definition be zero and hence so must *KAPWORSYS* (MC8.2)

**Slack Equations**

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$$TOTSAV_r = INVEST_r + WALRAS_r \quad \forall r \in rgn \quad (MC8.1)$$

$$KAPWORSYS = \sum_r KAPWOR_r \quad \forall r \in rgn \quad (MC8.2)$$


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## Model Closure Conditions or Rules<sup>29</sup>

In mathematical programming terms the model closure conditions are, at their simplest, a matter of ensuring that the numbers of equations and variables are consistent. However, the economic theoretic dimensions of model closure rules are more complex, and, as would be expected in the context of an economic model, more important. The essence of model closure rules is that they define important and fundamental differences in perceptions of how an economic system operates (see Sen, 1963; Pyatt, 1987; Kilkenny and Robinson, 1990). The closure rules can be perceived as operating on two levels; on a general level whereby the closure rules relate to macroeconomic considerations, e.g., investment expenditure determined by the volume of savings or exogenously, and on a specific level where the closure rules are used to capture particular features of an economic system, e.g., the degree of intersectoral capital mobility.

This model allows for a range of both general and specific closure rules. The discussion below provides details of some of the options available with this formulation of the model by reference to the accounts to which the rules refer. However, as will become readily apparent there are many permutations available, and hence this discussion deals with the general principles rather than trying to define all possible permutations. The philosophy adopted in the implementation of this model is to define a (minimal) base closure for the replication of the base case and then impose closure changes within a loop in the experiment/simulation file. This approach allows substantial flexibility in the definition of policy simulations while simultaneously allowing sensitivity testing of the chosen model closures. For the base solution the choice of model closure is basically a neoclassical closure; the reason for choosing this closure is NOT a statement about its appropriateness, rather it is a closure that allows flexibility in model solution and hence simplifies the process of verifying that the model is correctly specified and calibrated.

### 5.1 Foreign Exchange Account Closure

For the world numéraire the exchange rate index for the reference regions (*EPRI*) is fixed (C1a), although a parameter, *numerchk*, is attached to allow for ease of checking the

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<sup>29</sup> The term model ‘closure’ is used generically here to cover all permutations including variations in market clearing conditions and macroeconomic closure conditions.

homogeneity of the model.<sup>30</sup> At the same time the exchange rate for Globe is fixed as equal to the world numéraire (C1b).

The default closure for the non-Globe regions involves an assumption that the nominal exchange rate is flexible. Hence the trade balances ( $KAPWOR_{rgn}$ ) for all non-Globe regions are fixed (C1c) and the exchange rate is flexible. The most straightforward alternative is to fix the exchange rates for all non-Globe regions (C1d) and unfix the trade balances. However, there are clearly a range of permutations whereby the exchange rates for some regions are flexible while for others they are fixed.<sup>31</sup>

### *Foreign Exchange Account Closure*

$$EPRI = \overline{EPRI0} * numerchk \tag{C1a}$$

$$ER_{"glo"} = \overline{EPRI0} * numerchk \tag{C1b}$$

$$KAPWOR_{rgn} = \overline{KAPWOR_{rgn}} . \tag{C1c}$$

$$ER_{rgn} = \overline{ER_{rgn}} \tag{C1d}$$

## 5.2 Capital Account Closure

This discussion of the closure rules for the capital account begins by abstracting from some of the complexities into interactions between different closure conditions. To ensure that aggregate savings equal aggregate investment, the determinants of either savings or investment must be fixed. The default closure for this account requires the assumption that savings rates are exogenously determined which involves fixing both the multiplicative savings rates adjusters ( $SADJ_r$ ) (C2a) and the additive savings rates adjusters ( $DSHH_r$ ) (C2b) and allowing the savings rates to be fixed – typically at their base rates. With such a savings-driven closure the value and volume of investment must be free to vary.

<sup>30</sup> In the base and model simulations, numerchk equals one. It is a parameter attached to the world numéraire and the regional numéraire (see C5a and C5b). To check for homogeneity, a value other than one should have no effect on real variables in the model.

<sup>31</sup> The option is provided in the programme to control choice of these, and several other, closures by selection of regions to assign to a set and its complement.

Choosing an investment-driven closure requires making two distinct choices; first, is the level investment to be determined in terms of volume, value or expenditure share of final demand, and second, will savings adjust in a multiplicative or additive mode. Clearly, again, it is possible that the choices will vary by region. If the investment volume adjuster ( $IADJ_r$ ) is fixed (C2c), then the value of investment expenditure might change due to changes in the prices of investment commodities ( $PQD_{c,r}$ ). If the value of investment ( $INVEST_r$ ) is fixed (C2d) then the value of savings must be free to adjust as must the actual volume of investment. The same applies if the shares of investment expenditures in final demand ( $INVESTSH_r$ ) are fixed (C2e).

### *Capital Account Closure*

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$$SADJ_r = \overline{SADJ_r} \tag{C2a}$$

$$DSHH_r = \overline{DSHH_r} \tag{C2b}$$

$$IADJ_r = \overline{IADJ_r} \tag{C2c}$$

$$INVEST_r = \overline{INVEST_r} \tag{C2d}$$

$$INVESTSH_r = \overline{INVESTSH_r} \tag{C2e}$$


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Fixing savings, and thus deeming the economy to be savings-driven, could be termed a Neo-Classical approach. Closing the economy by fixing investment however makes the model reflect a Keynesian investment-driven assumption for the operation of an economy.

However, there are potentially important interaction effects. Note that there are other sources of potential savings for region – the government and the trade balances. The magnitudes of these other savings sources can also be controlled through the closure rules (see below). Consequently, there will clearly be an important interdependence between the choices of closure rules for different accounts; the most obvious one to be aware of is the interaction between household savings rates and household income tax rates when tax rates are made flexible and the level of government savings/deficit is fixed.

### 5.3 Government Account Closure

The closure rules for the government account are slightly more complex because they are important components of the model that are used to investigate fiscal policy considerations. The base specification uses the assumption that government savings are a residual; when the determinants of government income, i.e., tax rates, remittances etc., and expenditure are ‘fixed’, government savings must be free to adjust.

Thus, in the base specification all the tax rates are fixed by declaring the tax rates as parameters and then fixing all the tax rate scaling factors (C3.1a – C3.1n). Consequently, any changes in tax revenue to the government are consequences of changes in the other variables that enter into the tax income equations (T2.1 to T2.6). Controlling the volumes of commodity demand ( $QGD_{c,r}$ ) in the base specification government expenditure is then achieved by fixing the volumes of commodity demand ( $QGD_{c,r}$ ) through the government demand adjuster ( $QGDADJ_r$ ) (T3.2a). Notice however that since prices are typically free to change it is necessary to ensure that both government expenditure ( $EG_r$ ) in (C3.2b) and the share of government expenditure in final demand ( $VGDSH_r$ ) in (C3.2c) must be flexible.

**Tax Rate and Revenue Closure**

$$TMADJ_r = \overline{TMADJ_r} \tag{C3.1a}$$

$$TEADJ_r = \overline{TEADJ_r} \tag{C3.1b}$$

$$TSADJ_r = \overline{TSADJ_r} \tag{C3.1c}$$

$$TVADJ_r = \overline{TVADJ_r} \tag{C3.1d}$$

$$TXADJ_r = \overline{TXADJ_r} \tag{C3.1e}$$

$$TYFADJ_r = \overline{TYFADJ_r} \tag{C3.1f}$$

$$TYHADJ_r = \overline{TYHADJ_r} \tag{C3.1g}$$

$$TFADJ_r = \overline{TFADJ_r} \tag{C3.1h}$$

$$DTM_r = \overline{DTM_r} \tag{C3.1i}$$

$$DTE_r = \overline{DTE_r} \tag{C3.1j}$$

$$DTS_r = \overline{DTS_r} \tag{C3.1k}$$

$$DTX_r = \overline{DTX_r} \tag{C3.1l}$$

$$DTYF_r = \overline{DTYF_r} \tag{C3.1m}$$

$$DTYH_r = \overline{DTYH_r} \tag{C3.1n}$$

$$DTF_r = \overline{DTF_r} \tag{C3.1o}$$

This specification ensures that all the parameters that the government can/does control are fixed and consequently that the only determinants of government income and expenditure that are free to vary are those that the government does not directly control. Hence the equilibrating condition is that government savings, the internal balance ( $KAPGOV_r$ ), is not fixed in (C3.2d).

The number of possible permutations for closing the government account for each region is consequently substantial. Practical experience indicates that great care is needed when adjusting the government closure rules to avoid both unbalancing the model and

imposing closure rules that are contradictory.<sup>32</sup> A common change is to require that the government's savings/deficit is fixed; this requires fixing  $KAPGOV_r$  in C3.2d, in which case either government income or expenditure must be free to adjust. Such a condition might reasonably be expected in many circumstances, e.g., the government might define an acceptable level of borrowing, or such a condition might be imposed externally.

### ***Government Expenditure and Savings Closure***

$$QGDADJ_r = \overline{QGDADJ_r} \tag{C3.2a}$$

$$EG_r = \overline{EG_r} \tag{C3.2b}$$

$$VGDSH_r = \overline{VGDSH_r} \tag{C3.2c}$$

$$KAPGOV_r = \overline{KAPGOV_r} \tag{C3.2d}$$

In its simplest form this can be achieved by allowing one of the previously fixed tax rate adjusters (C3.1a to C3.1n) to vary. Thus, if the sales tax adjuster ( $TSADJ_r$ ) is made variable then the sales tax rates will be varied equiproportionately so as to satisfy the internal balance condition. More complex experiments might result from the imposition of multiple conditions, e.g., a halving of import duty rates coupled with a reduction in government deficit, in which case the variables  $TMADJ_r$  and  $KAPGOV_r$  would also require resetting. But these conditions might create a model that is infeasible, e.g., due to insufficient flexibility through the import duties mechanism, or unrealistically high rates of sales taxes. In such circumstances it may be necessary to allow adjustments in multiple tax adjusters. One method then would be to fix the tax adjusters to move in parallel with each other.

However, if the adjustments only take place through the tax rate scaling factors the relative tax rates will be fixed. To change relative tax rates, it is necessary to change the relevant tax parameters. Such changes would be implemented in policy experiment files by changing the values of the parameters that determine relative tax rates.

<sup>32</sup> The most common problems with contradictory government closure rules relate to the interactions between the government and capital (investment) accounts, in particular when a combination of flexible savings and tax rates producing mutually contradictory effects.

Note also that as with the investment account, there is a needed care over setting the constraints on government demand. If the government demand volume adjuster ( $QGDADJ_r$ ) is fixed (C3.2a), then the value of government expenditure might change due to changes in the prices of commodities ( $PQD_{c,r}$ ). If the value of government expenditure ( $EG_r$ ) is fixed (C3.2b) then both government savings must be free to adjust as must the actual volume of expenditure, when tax rates are exogenous. The same applies if the shares of government expenditures in final demand ( $VGDSH_r$ ) are fixed (C3.2e).

#### 5.4 Technology and Efficiency

The default assumption in the model is that efficiency, commonly called technology, is fixed. Hence the shift parameters are assumed to be constant.

##### *Technology Parameter Closure*

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$$ADXADJ_r = \overline{ADXADJ0_r} \quad (C4.3a)$$

$$DADX_r = \overline{DADX0_r} \quad (C4.3b)$$

$$ADVAADJ_r = \overline{ADVAADJ0_r} \quad (C4.4c)$$

$$DADVA_r = \overline{DADVA0_r} \quad (C4.4d)$$

$$ADFDfADJ_f = \overline{ADFDfADJ0_f} \quad (C4.5e)$$

$$ADFDaADJ_a = \overline{ADFDaADJ0_a} \quad (C4.5f)$$

$$ADFDrADJ_r = \overline{ADFDrADJ0_r} \quad (C4.5g)$$


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Changes in efficiency can either be imposed exogenously or a technology variable can be freed up so as to satisfy some other condition, e.g., the required efficiency gain needed to satisfy a predetermined increase in GDP.

#### 5.5 Numéraire

The model specification allows for a choice between two price normalisation equations, the consumer price index ( $CPI_r$ ) and a producer price index ( $PPI_r$ ). A *numéraire* is needed for

each region, to serve as a base since the model is homogenous of degree zero in prices for each region, and hence only defines relative prices.

### *Numéraire Closure*

$$CPI_r = \overline{CPI_r} * numerchk \tag{C5a}$$

$$PPI_r = \overline{PPI_r} * numerchk \tag{C5b}$$

## 5.7 Factor Market Closure

The factor market closure rules are more difficult to implement than many of the other closure rules. Hence the discussion below proceeds in three stages; the first stage sets up a basic specification whereby all factors are deemed perfectly mobile, the second stage introduces a more general specification whereby factors can be made activity specific and allowance can be made for unemployed factors, while the third stage introduces the idea that factor market restrictions may arise from activity specific characteristics, rather than the factor inspired restrictions considered in the second stage.

### 5.7.1 Full Factor Mobility and Employment Closure

This factor market closure requires that the total supply of and total demand for factors equate, and since the total supplies of each factor are determined exogenously this condition is satisfied by the equilibrium condition (C6.1a). The demands for factor  $f$  by activity  $a$  in region  $r$  and the wage rates for factors are determined endogenously. But the model specification includes the assumption that the wage rates for factors are averages ( $WF_{f,r}$ ), by allowing for the possibility that the payments to notionally identical factors might vary across activities, due to activity specific ‘efficiency’ factors ( $WFDIST_{f,a,r}$ ) through the variable that captures the ‘sectoral proportions for factor prices’. Since these proportions are assumed to be a consequence of the use made by activities of factors, rather than of the factors themselves, they are therefore assumed fixed (C6.1b). And finally bounds are placed upon the average factor prices, (C6.1c), so that meaningful results are produced.

**Full Employment and Mobile Factors**

$$FS_{f,r} = \overline{FS}_{f,r} \quad (C6.1a)$$

$$WFDIST_{f,a,r} = \overline{WFDIST}_{f,a,r} . \quad (C6.1b)$$

$$\text{Min } WF_{f,r} = 0 \quad (C6.1c)$$

$$\text{Max } WF_{f,r} = +\text{infinity}$$

5.7.2 Factor Immobility and/or Unemployment Closures

More general factor market closures wherein factor immobility and/or factor unemployment are assumed can be achieved by determining which of the variables referring to factors are treated as variables and which of the variables are treated as fixed. If factor market closure rules are changed it is important to be careful to preserve the equation and variable counts when relaxing conditions, i.e., converting parameters into variables, and imposing conditions, i.e., converting variables into parameters, while preserving the economic logic of the model.

A convenient way to proceed is to define a block of conditions for each factor. For this model this amounts to defining the following possible equations (C6.2a) where *fact* indicates the specific factor and *activ* a specific activity. This block of equations includes all the variables that were declared for the model with reference to factors plus extra equations for  $WFDIST_{fact,activ,r}$ , i.e.,  $WFDIST_{fact,activ,r} = \overline{WFDIST}_{fact,activ,r}$ , whose role will be defined below.

The choice of which equations are binding and which are not imposed will determine the factor market closure conditions.

**Factor Unemployment Closure**

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$$\begin{aligned}
 FS_{fact,r} &= \overline{FS}_{fact,r} \\
 WFDIST_{fact,a,r} &= \overline{WFDIST}_{fact,a,r} \\
 \text{Min } WF_{fact,r} &= 0 \\
 \text{Max } WF_{fact,r} &= +\text{infinity} \\
 FD_{fact,a,r} &= \overline{FD}_{fact,a,r} \\
 WF_{fact,r} &= \overline{WF}_{fact,r} \\
 WFDIST_{fact,activ,r} &= \overline{WFDIST}_{fact,activ,r} \\
 \text{Min } FS_{fact,r} &= 0 \\
 \text{Max } FS_{fact,r} &= +\text{infinity}
 \end{aligned}
 \tag{C6.2a}$$


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As can be seen the first four equations in the block (C6.2a) are the same as those in the ‘Full Factor Mobility and Employment Closure’; hence ensuring that these four equations are operating for each of the factors is a longhand method for imposing the ‘Full Factor Mobility and Employment Closure’. Assume that this set of conditions represents the starting points, i.e., the first four equations are binding and the last five equations are not imposed.

Assume now that it is planned to impose a short run closure on the model, whereby a factor is assumed to be activity specific, and hence there is no inter sectoral factor mobility. Typically this would involve making capital activity specific and immobile, although it can be applied to any factor. This requires imposing the condition that factor demands are activity specific, thus (C6.3a) must be imposed. But the returns to this factor in different uses (activities) must now be allowed to vary, i.e., (C6.3b) must now be relaxed.

**Activity Specific and Immobile Factor**

$$FD_{fact,a,r} = \overline{FD}_{fact,a,r} \tag{C6.3a}$$

$$WFDIST_{fact,a,r} = \overline{WFDIST}_{fact,a,r} \tag{C6.3b}$$

$$FS_{fact,r} = \overline{FS}_{fact,r} \tag{C6.3c}$$

$$WFDIST_{fact,activ,r} = \overline{WFDIST}_{fact,activ,r} \tag{C6.3d}$$

The number of imposed conditions is equal to the number of relaxed conditions, which suggests that the model will still be consistent. But the condition fixing the total supply of the factor is redundant since if factor demands are fixed the total factor supply cannot vary. Hence the condition (C6.3a) is redundant and must be relaxed. Hence at least one other condition must be imposed to restore balance between the numbers of equations and variables. This can be achieved by fixing one of the sectoral proportions for factor prices for a specific activity, i.e., (C6.3d), which means that the activity specific returns to the factor will be defined relative to the return to the factor in *activ*.<sup>33</sup>

Start again from the closure conditions for full factor mobility and employment and then assume that there is unemployment of one or more factors in the economy; typically this would be one type or another of unskilled labour. If the supply of the unemployed factor is perfectly elastic, then activities can employ any amount of that factor at a fixed price. This requires imposing a condition that fixes the wage rate, (C6.4a) and relaxing the assumption that the total supply of the factor is fixed at the base level, i.e., relaxing (C6.4b).

It is useful however to impose some restrictions on the total supply of the factor that is unemployed. Hence the conditions (C6.4c) can be imposed.<sup>34</sup>

<sup>33</sup> It can be important to ensure a sensible choice of reference activity. This is important if a factor is not used, or little used, by the chosen activity.

<sup>34</sup> If the total demand for the unemployed factor increases unrealistically in the policy simulations, then it is possible to place an upper bound of the supply of the factor and then allow the wage rate from that factor to vary.

### *Unemployment of a Specific Factor*

$$WF_{fact,r} = \overline{WF}_{fact,r} \quad (C6.4a)$$

$$FS_{fact,r} = \overline{FS}_{fact,r} \quad (C6.4b)$$

$$\text{Min } FS_{fact,r} = 0 \quad (C6.4c)$$

$$\text{Max } FS_{fact,r} = +\text{infinity}$$

#### 5.7.3 Activity Inspired Restrictions on Factor Market Closures

There are circumstances where factor use by an activity might be restricted as a consequence of activity specific characteristics. For instance it might be assumed that the volume of production by an activity might be predetermined, e.g., known mineral resources might be fixed and/or there might be an exogenously fixed restriction upon the rate of extraction of a mineral commodity. In such cases the objective might be to fix the quantities of all factors used by an activity, rather than to fix the amounts of a factor used by all activities. This is clearly a variation on the factor market closure conditions for making a factor activity specific.

If all factors used by an activity are fixed, this requires imposing the conditions C6.5a, where *activ* refers to the activity of concern. But the returns to these factors in these activities must now be allowed to vary, i.e., the conditions (C6.5b) must now be relaxed. In this case the condition fixing the total supply of the factor is not redundant since only the factor demands by *activ* are fixed and the factor supplies to be allocated across other activities are the total supplies unaccounted for by *activ*.

**Fixed Factor Use**

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$$FD_{f,activ,r} = \overline{FD}_{f,activ,r} \quad (C6.5a)$$

$$WFDIST_{f,activ,r} = \overline{WFDIST}_{f,activ,r} \quad (C6.5b)$$


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Such conditions can be imposed by extending the blocks of equations for each factor in the factor market closure section. However, it is often easier to manage the model by gathering together factor market conditions that are inspired by activity characteristics after the factor inspired equations. In this context it is useful to note that when working in GAMS that the last condition imposed, in terms of the order of the code, is binding and supersedes previous conditions.

## Implementation and Complementary Programmes

The current version of the model is implemented as a mixed complementarity problem (MCP) in GAMS 250 21.5 using the Path solver. In a model with 15 sectors, 4 factors and 14 regions, which generates some 24,000 equations and variables, the initial, or replication, solve takes some 15 seconds on a well-equipped Pentium 4 2.6MHz PC, while the entire run for a series of 11 simple experiments run in a loop takes about 75 seconds, including writing out a comprehensive set of results to a series of GDX files.

However once a programme is established the time consuming activities are those associated with the generation of new aggregations and the analyses of results. In order to address these problems as pair of Excel based programmes, using VBA, and a series of GAMS programmes have been developed.

### 6.1 Database Aggregation

The Excel based programme for aggregating the database is called SAMGator (PROVIDE, 2004b). This is general aggregation programme that uses Excel to provide a front end that simplifies the creation of the set files required for the mapping aggregations. The user declares, with descriptors, the accounts required in the new aggregation and identifies those accounts in the database that will be aggregated to form the new accounts; this is all done using point and click commands in an Excel worksheet. Once all the new accounts have been declared and assigned, and provided all the data in the original database are accounted for, a command triggers the creation of the mapping files. Finally the user triggers the running of the aggregation programme from within Excel. At this point SAMGator generates a GAMS programme file, \*.gms, runs that programme and writes out the results to GDX and/or Excel.

### 6.2 Analyses of Results

The management and organisation of results from large CGE models can be both time consuming and confusing due to the large number of data points generated, e.g., the model with 15 sectors, 4 factors and 14 regions when run with 11 experiments generates more than 500,000 data points even when only running a limited set of analyses programmes. An Excel based programme for analysing, organising and summarising results from CGE models called

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SeeResults (PROVIDE, 2004a) has been developed for the interactive reading of GAMS model results that have been stored in GDX format.

The GDX format is technically superlative, with GDX files being both extremely fast and small. Once the result data are in GDX format, they can be viewed using GAMSIDE or GDXViewer, a specialised utility for viewing GDX files and both of these include basic facilities for changing data orientation and the GDXViewer also includes basic charting (plot) facilities. While these are useful, there are a number of limitations. Filtering ability is limited, which can make it difficult to compare results within a smaller subset of elements from a large set. Charting facilities in GDXViewer are limited and not designed for presentation quality output. It is not possible to manipulate data, change formatting, perform calculations or cut and paste data to other applications, although there are data output facilities. In short, these facilities are suitable for viewing raw data initially but are not a complete solution for the processing of model results.

Among proprietary programmes Excel is the logical choice; it has reasonably good charting facilities, is excellent for general data manipulation and provides the means to format data for presentation purposes. It can also provide limited database functionality such as reorientation and filtering via the pivot table feature. It is also useful as a means to distribute data, because it has a (very) wide user base. But it is often tedious getting large amounts of data into Excel and can produce extremely large files that are difficult to transfer. SeeResults automates much of this process; it avoids overly large Excel files by working interactively with GDX files, that remain the files in which data are stored, and coordinates information that assists with the categorisation, classification and labeling of the results.

The guiding principle behind SeeResults is to make use of the functionality of GDX and Excel; thereby avoiding the need to develop additional standalone programme. Excel is conceptually a very powerful programming environment, allowing use of the spreadsheet itself as a data construct and combining the power of Visual Basic with the ability to use spreadsheet functions in Visual Basic code. A major usage of Excel functionality is the use of Pivot Tables for data reorientation and filtering in multidimensional data. Excel's pivot tables are ideally suited to the task of storing and presenting reasonable amounts of data and allowing the display format to be changed after data has been imported to Excel. It performs

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SeeResults technically demanding data handling tasks more efficiently than would have been possible using custom Visual Basic code.

## **Concluding Comments**

This paper has described the variant of the ANARRES model used in online training programmes. The model described here contains relatively simple behavioural relationships although it requires a programme that contains a number of technically sophisticated features. Moreover it is capable of being implemented with any aggregation of the GTAP database. This version of the model is made available to participants in Global CGE Modelling course offered by [cgemod.org.uk](http://cgemod.org.uk).

## Appendices

### A1. ANARRES Model Genealogy

The GLOBE model project started in June 2002 at a conference on *Poverty, Trade & Tools for Development*, which was hosted by the International Food Policy Research Institute in honour of Sherman Robinson's 60<sup>th</sup> birthday. During that conference Karen Thierfelder and Scott McDonald discussed, and agreed on, the creation of a SAM based global CGE model calibrated using the GTAP database. Karen and Scott had both 'learnt' CGE models starting with version of a single country CGE model developed for the US Department of Agriculture's (USDA) Economic Research Service (ERS) under the leadership of Sherman Robinson (Robinson *et al.*, 1990; Kilkenny, 1991). Karen had worked on the NAFTA project, also led by Sherman Robinson, and had subsequently used a global model that was descended from the NAFTA model. Scott had been introduced to GTAP by Terrie Walmsley and had used SAMs derived from the GTAP database for teaching single country CGE modelling. These teaching models and the PROVIDE project model (McDonald, 2003) provided the core single country code used to develop the GLOBE model.<sup>35</sup>

The first full versions of the model were in use by late 2004 (the womod7\*.gms series) while the first formal documentation (McDonald, Robinson and Thierfelder, 2007) appeared in May 2007 (based on the womod9\*.gms series) as a working paper from the US Naval Academy (working paper 14). Subsequent developments continued until late 2009 when the technical documentation and user guide (McDonald and Thierfelder) were revised and an open source version of the model, GLOBE v1, was made available (glb1.gms). Model developments since late 2009 were consolidated to produce GLOBE v2, which also formed the base for GLOBE\_DYN.

There are currently several variants of the GLOBE model: GLOBE\_EN (energy model), GLOBE\_MIG (migration model), GLOBE\_IMP (imperfect competition) and other less formal variants developed as parts of various research activities. Current developments of the

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<sup>35</sup> The IFPRI standard model (Lofgren *et al.*, 2001) was also a descendant of the USDA's ERS model. Both Karen and Scott were in close contact with the team at IFPRI during the development of the IFPRI standard model and aspects of that model have clearly influenced both the GLOBE and STAGE models.

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GLOBE model family, as GLOBE v3, are on-going; an objective of this exercise is to consolidate several of the variants into a single version.

The ANARRES model is a development of the GLOBE\_3 model that includes many of the features found in variants of the GLOBE model as options.

The ANARRES model is part of a suite of models that include a single country model (STAGE – a development of the PROVIDE model that was developed from the USDA ERS model) and a range of teaching models – the SMOD suite, STAGE\_t and ANARRES\_t. All these models use a (overwhelmingly) common set of notation and formats.

**A2 Equation and Variable Counts for the ANARRES CGE Model**

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>EXPORTS BLOCK</b>					
$PEDEF_{c,r}$	$PE_{c,r} * QE_{c,r} = \sum_w PER_{c,w,r} * QER_{c,w,r} \quad \forall c \in ce, r \in rgn$	$(ce * rgn)$	$PE_{c,r}$	$(ce * rgn)$	NO
$PERDEF2_{c,w,r}$	$PER_{c,w,r} = PWE_{c,w,r} * ER_r * (1 - TE_{c,w,r}) \quad \forall c \in cer$	$(cer * w * r)$	$PER_{c,r,w}$	$(cer * w * r)$	NO
$PERDEFHG_{c,w,r}$	$PER_{c,w,r} = PE_{c,r} \quad \forall c \in ct2, r \notin rgn, w \in wgn$	$(ct2 * w * 1)$		$(ct2 * w * 1)$	YES
$CET_{c,r}$	$QXC_{c,r} = at_{c,r} * (\gamma_{c,r} * QE_{c,r}^{\rho_{c,r}^t} + (1 - \gamma_{c,r}) * QD_{c,r}^{\rho_{c,r}^t})^{\frac{1}{\rho_{c,r}^t}}$ $\forall c \in (cd \cap ce), r \in rgn$	$(c * rgn)$	$QD_{c,r}$	$(c * rgn)$	NO
$ESUPPLY_{c,r}$	$QE_{c,r} = QD_{c,r} \left[ \frac{PE_{c,r} * (1 - \gamma_{c,r})}{PD_{c,r} * \gamma_{c,r}} \right]^{\frac{1}{(\rho_{c,r}^t - 1)}} \quad \forall c \in (cd \cap ce), r \in rgn$	$(c * rgn)$	$QE_{c,r}$	$(c * rgn)$	NO
$CETALT_{c,r}$	$QXC_{c,r} = QD_{c,r} + QE_{c,r} \quad \forall (c \in (cd \cap cen), r \in rgn)$ OR $\forall (c \in (cdn \cap ce), r \in rgn)$				NO
$CETLEV2_{c,w,r}$	$QER_{c,w,r} = QE_{c,r} * \left( \frac{PER_{c,w,r}}{\left( (PE_{c,r} * \gamma_{c,w,r}^r * at_{c,r}^r)^{\rho_{c,r}^e} \right)} \right)^{\frac{1}{(\rho_{c,r}^e - 1)}}$ $\forall c \in cer2, r \in rgn$	$(cer * rgn * w)$	$QER_{c,r,w}$	$(cer * rgn * w)$	NO



Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>IMPORTS BLOCK</b>					
$CETREQ_{c,r}$	$QE_{c,r} = \sum_w QER_{c,w,r} \quad \forall c \in ct, r \notin rgn$	$(ct*1)$	$QE_{c,r}$	$(ct*1)$	YES
$TSHIP_{c,r}$	$QE_{c,r} = QM_{c,r} \quad \forall c \in ct2, r \notin rgn$	$(ct2*1)$	$QE_{c,r}$	$(ct2*1)$	YES
$PMLDEF_{c,r}$	$PML_{c,r} = \frac{\sum_{w \in cmr} (PMR_{w,c,r} * QMR_{w,c,r})}{QML_{c,r}} \quad \forall (c,r) \in cml$	$(cml*r)$	$PML$	$(cml*r)$	YES
$PMSDEF_{c,r}$	$PMS_{c,r} = \sum_w ioqmrqms_{w,c,r} * PMR_{w,c,r} \quad \forall (c,r) \in cms$	$(cms*r)$	$PMS$	$(cms*r)$	YES
$PMRDEF2_{w,c,r}$	$PMR_{w,c,r} = PWM_{w,c,r} * ER_r * (1 + TM_{w,c,r}) + TMS_{w,c,r} \quad \forall c \in cmr$	$(cmr*r*w)$	$PMR_{w,c,r}$	$(cmr*r*w)$	YES
$PMDEF_{c,r}$	$PM_{c,r} * QM_{c,r} = (PML_{c,r} * QML_{c,r}) + (PMS_{c,r} * QMS_{c,r}) \quad \forall (c,r) \in cm_{c,r}$	$(cm*r)$	$PM_{c,r}$	$(cm*r)$	YES
$PWMDEF_{w,c,r}$	$PWM_{w,c,r} = PWMFOB_{w,c,r} + \left( \sum_{cp \in ct_{cp,r}} margcor_{w,cp,c,r} * PT_{cp,r} \right) \quad \forall c \in cmr$	$(cmr*r*w)$	$PWM_{c,r,w}$	$(cmr*r*w)$	YES

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>IMPORTS BLOCK</b>					
$ARMINGTON_{c,r}$	$QQ_{c,r} = ac_{c,r} \left( \delta_{c,r} * QM_{c,r}^{-\rho_{c,r}^c} + (1 - \delta_{c,r}) * QD_{c,r}^{-\rho_{c,r}^c} \right)^{-\left(\frac{1}{\rho_{c,r}^c}\right)}$ $\forall c \in (cx \cap cm), r \in rgn$	$(c * rgn)$	$QM_{c,rgn}$	$(c * rgn)$	NO
$COSTMIN_{c,r}$	$QM_{c,r} = QD_{c,r} * \left( \left( \frac{PD_{c,r}}{PM_{c,r}} \right) * \left( \frac{\delta_{c,r}}{(1 - \delta_{c,r})} \right) \right)^{\frac{1}{(1 + \rho_{c,r}^c)}}$ $\forall c \in (cx \cap cm), r \in rgn$	$(c * rgn)$	$PD_{c,rgn}$	$(c * rgn)$	NO
$ARMALT_{c,r}$	$QQ_{c,r} = QD_{c,r} + QM_{c,r}$ $\forall c \in (cx \cap cmn), r \in rgn$ OR $\forall c \in (cxn \cap cm), r \in rgn$				NO
$QMSEQ_{c,r}$	$QMS_{c,r} = ioqmsqm_{c,r} + QM_{c,r}$ $\forall c \in cms$	$(cms * r)$	$QMS_{c,r}$	$(cms * r)$	YES
$QMLEQ_{c,r}$	$QML_{c,r} = ioqmlqm_{c,r} + QM_{c,r}$ $\forall c \in cml$	$(cml * r)$	$QML_{c,r}$	$(cml * r)$	YES
$QMREQ_{w,c,r}$	$QMR_{w,c,r} = ioqmrqms_{w,c,r} + QMS_{c,r}$ $\forall c \in cmrs$				YES
$ARMLEV2_{w,c,r}$	$QMR_{w,c,r} = QML_{c,r} * \left( \frac{PMR_{w,c,r} * acr_{c,r}^{\rho_{c,r}^m}}{PML_{c,r} * \delta_{w,c,r}^r} \right)^{\left(\frac{-1}{(\rho_{c,r}^m + 1)}\right)}$ $\forall c \in cmrl (w * c * r)$	$(w * c * r)$	$QMR_{w,c,r}$	$(w * c * r)$	YES
$QTEQ_{w,c,r}$	$QT_{w,c,r} = \sum_{cp} (QMR_{w,cp,r} * margcor_{w,c,cp,r})$ $\forall c \in ct2, r \in rgn$	$(ct2 * rgn * w)$	$QT_{c,rgn,w}$	$(ct2 * rgn * w)$	NO

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>COMMODITY PRICE BLOCK</b>					
			$PD_c$		
$PQSDEF_{c,r}$	$PQS_{c,r} = \frac{(PD_{c,r} * QD_{c,r}) + (PM_{c,r} * QM_{c,r})}{QQ_{c,r}}$	$\forall c \in (cd \cup cm), r \in (g^*rgn)$	$PQS_{c,r}$	$(c*rgn)$	NO
$PQDDEF_{c,r}$	$PQD_{c,r} = PQS_{c,r} * (1 + TS_{c,r})$	$\forall c \in (cd \cup cm), r \in rgn$	$PQD_{c,r}$	$(c*rgn)$	NO
$PQCDDEF_{c,r}$	$PQCD_{c,r} = PQD_{c,r} * (1 + TV_{c,r})$	$\forall c \in (cd \cup cm), r \in rgn$	$PQCD_{c,r}$	$(c*rgn)$	NO
$PXCDEF_{c,r}$	$PXC_{c,r} = \frac{(PD_{c,r} * QD_{c,r}) + (PE_{c \in ce,r} * QE_{c \in ce,r})}{QXC_{c,r}}$	$\forall c \in cx, r \in rgn$	$PXC_{c,r}$	$(cx*rgn)$	NO
<b>NUMERAIRE PRICE BLOCK</b>					
$CPIDEF_r$	$CPI_r = \sum_c vqcdsh_{c,r} * PQD_{c,r}$	$\forall r \in rgn$	$CPI_r$	$rgn$	NO
$PPIDEF_r$	$PPI_r = \sum_c vqdsh_{c,r} * PD_{c,r}$	$\forall r \in rgn$	$PPI_r$	$rgn$	NO
$ERPIDEF$	$ERPI = \sum_{ref} vqesh_{ref} * ER_{ref}$		$ERPI$	1	NO

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>PRODUCTION BLOCK – TOP LEVEL</b>					
$PXDEF_{a,r}$	$PX_{a,r} = \sum_c ioqxcqx_{a,c,r} * PXC_{c,r} \quad \forall r \in rgn$	$(a*rgn)$	$PX_{a,r}$	$(a*rgn)$	NO
$PVADEF_{a,r}$	$PX_{a,r} * (1 - TX_{a,r}) * QX_{a,r} = (PVA_{a,r} * QVA_{a,r}) + (PINT_{a,r} * QINT_{a,r}) \quad \forall r \in rgn$	$(a*rgn)$	$PVA_{a,r}$	$(a*rgn)$	NO
$PINTDEF_{a,r}$	$PINT_{a,r} = \sum_c ioqint_{c,a,r} * PQD_{c,r} \quad \forall r \in rgn$	$(a*rgn)$	$PINT_{a,r}$	$(a*rgn)$	NO
$ADXEQ_{a,r}$	$ADX_{a,r} = ((adxb_{a,r} + dabadx_{a,r}) * ADXADJ_r) + (DADX_r * adx01_{a,r})$	$(a*rgn)$	$ADX_{a,r}$	$(a*rgn)$	NO
$QXPRODFN_{a,r}$	$QX_{a,r} = ADX_{a,r} * \left[ \delta_{a,r}^x * (QVA_{a,r})^{-\rho_{a,r}^x} + (1 - \delta_{a,r}^x) * (QINT_{a,r})^{-\rho_{a,r}^x} \right]^{1/\rho_{a,r}^x} \quad \forall r \in rgn, a \in aqx$	$(aqx*rgn)$	$QX_{a,r}$	$(aqx*rgn)$	NO
$QXFOC_{f,a,r}$	$QVA_{a,r} = QINT_{a,r} * \left( \left( \frac{PINT_{a,r}}{PVA_{a,r}} \right) * \left( \frac{\delta_{a,r}^x}{(1 - \delta_{a,r}^x)} \right) \right)^{\left( \frac{1}{1 + \rho_{a,r}^x} \right)} \quad \forall r \in rgn, a \in aqx$	$(aqx*rgn)$	$QINT_{a,r}$	$(aqx*rgn)$	NO
$QINTDEF_{a,r}$	$QINT_{a,r} = \sum_a ioqintqx_{a,r} * QX_{a,r} \quad \forall r \in rgn, a \in aqxn$	$(aqxn*rgn)$	$QX_{a,r}$	$(aqxn*rgn)$	NO
$QVADEF_{a,r}$	$QVA_{a,r} = \sum_a ioqvaqx_{a,r} * QX_{a,r} \quad \forall r \in rgn, a \in aqxn$	$(aqxn*rgn)$	$QINT_{a,r}$	$(aqxn*rgn)$	NO
$COMOUT_{c,r}$	$QXC_{c,r} = \sum_a ioqxcqx_{a,c,r} * QX_{a,r} \quad \forall r \in rgn$	$(c*rgn)$	$QXC_{c,r}$	$(c*rgn)$	NO

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>PRODUCTION BLOCK – SECOND LEVEL</b>					
$ADVAEQ_{a,r}$	$ADVA_{a,r} = ((advab_{a,r} + dabadva_{a,r}) * ADVAADJ_r) + (DADVA_r * adva01_{a,r})$	$(a*rgn)$	$ADVA_{a,r}$	$(a*rgn)$	NO
$QVAPRODFN_{a,r}$	$QVA_{a,r} = ADVA_{a,r} * \left( \sum_{f2} \delta_{f2,a,r}^{va} * (ADFD_{f,a,r} * FD_{f2,a,r})^{-\rho_{a,r}^{va}} \right)^{\left( \frac{-1}{\rho_{a,r}^{va}} \right)}$	$(a*rgn)$	$QVA_{a,r}$	$(a*rgn)$	NO
	$\forall r \in rgn$				
$QVAFOC_{f,a,r}$	$WF_{ff,r} * WFDIST_{ff,a,r} * (1 + TF_{ff,a,r})$ $= PVA_{a,r} * QVA_{a,r} * \left[ \sum_{ff} \delta_{ff,a,r}^{va} * (ADFD_{ff,a,r} * FD_{ff,a,r})^{-\rho_{a,r}^{va}} \right]^{(-1)}$ $* \delta_{ff,a,r}^{va} * (ADFD_{ff,a,r})^{-\rho_{a,r}^{va}} * (FD_{ff,a,r})^{(-\rho_{a,r}^{va}-1)}$	$(f*a*rgn)$	$FD_{a,f,r}$	$(f*a*rgn)$	NO
	$\forall r \in rgn, ff \in f, \delta_{ff,a,r}^{va} > 0$				
$QINTDEQ_{c,r}$	$QINTD_{c,r} = \sum_a ioqint_{c,a,r} * QINT_{a,r}$	$(c*rgn)$	$QINTD_{c,r}$	$(c*rgn)$	NO
	$\forall r \in rgn, cintd_{c,r}$				

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>PRODUCTION BLOCK – THIRD LEVEL</b>					
$ADFDEQ_{f,a,r}$	$ADFD_{f,a,r} = \left( \begin{array}{l} (adfdb_{f,a,r} + dabadfd_{f,a,r}) \\ *ADFDfADJ_f * AFDaADJ_a * AFDDrADJ_r \end{array} \right)$				
$FDPRODFN_{ff,a,r}$	$FD_{ff,a,r} = ADFAG_{ff,a,r} * \left( \sum_l \delta_{ff,l,a,r}^{fd} * (FD_{l,a,r})^{\rho_{ff,a,r}^{fd}} \right)^{\left( \frac{-1}{\rho_{ff,a,r}^{fd}} \right)}$ <p style="text-align: center;"><math>\forall r \in rgn, \delta_{ff,l,a,r}^{fd}, ff \in fag</math></p>				
	$WF_{l,r} * WFDIST_{l,a,r} * (1 + TF_{l,a,r})$ $= WF_{ff,r} * WFDIST_{ff,a,r} * (1 + TF_{ff,a,r}) * FD_{ff,a,r}$				
$FDFOC_{ff,f3,a,r}$	$* \left[ \sum_l \delta_{ff,l,a,r}^{fd} * FD_{l,a,r}^{-\rho_{ff,a,r}^{fd}} \right]^{(-1)} * \delta_{ff,l,a,r}^{fd} * FD_{l,a,r}^{(-\rho_{ff,a,r}^{fd}-1)}$ <p style="text-align: center;"><math>\forall r \in rgn, \delta_{ff,l,a,r}^{fd}, ff \in fag</math></p>				



Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>FACTOR BLOCK</b>					
$YFEQ_{f,r}$	$YF_{f,r} = \sum_a WF_{f,r} * WFDIST_{f,a,r} * FD_{f,a,r} \quad \forall r \in rgn$	$(f*rgn)$	$YF_{f,r}$	$(f*rgn)$	NO
$YFDISTEQ_{f,r}$	$YFDIST_{f,r} = (YF_{f,r} - (deprec_{f,r} * YF_{f,r})) * (1 - TYF_{f,r})$ $\forall r \in rgn$	$(f*rgn)$	$YFDIST_{f,r}$	$(f*rgn)$	NO
<b>HOUSEHOLD BLOCK</b>					
$YHEQ_{h,r}$	$YH_{h,r} = \sum_f hvas_{h,f,r} * YFDIST_{f,r} \quad \forall r \in rgn$	$(h*rgn)$	$YH_{h,r}$	$(h*rgn)$	NO
$HEXPEQ_{h,r}$	$HEXP_{h,r} = (YH_{h,r} * (1 - TYH_{h,r})) * (1 - SHH_{h,r})$ $QCD_{c,h,r} * PQCD_{c,r} = (PQCD_{c,r} * qcdconst_{c,h,r})$	$\forall r \in rgn$ $(h*rgn)$	$HEXP_r$	$(h*rgn)$	NO
$QCDEQ_{c,h,r}$	$+ \beta_{c,h,r} * (HEXP_{h,r} - \sum_c PQCD_{c,r} * qcdconst_{c,h,r})$ $\forall r \in rgn$	$(c*h*rgn)$	$QCD_{c,h,r}$	$(c*h*rgn)$	NO



Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>GOVERNMENT TAXES BLOCK</b>					
$TEDEF_{c,w,r}$	$TE_{c,w,r} = \left( (teb_{c,w,r} + dabte_{c,w,r}) * TEADJ_r \right) + (DTE_r * te01_{c,w,r})$ $\forall c \in cer$	$(cer*r*w)$	$TE_{c,r,w}$	$(cer*r*w)$	NO
$TMDEF_{w,c,r}$	$TM_{w,c,r} = \left( (tmb_{w,c,r} + dabtm_{w,c,r}) * TMADJ_r \right) + (DTM_r * tm01_{w,c,r})$ $\forall c \in cmr$	$(cmr*r*w)$	$TM_{c,r,w}$	$(cmr*r*w)$	NO
$TSDEF_{c,r}$	$TS_{c,r} = \left( (tsb_{c,r} + dabts_{c,r}) * TSADJ_r \right) + (DTS_r * ts01_{c,r})$ $\forall r \in rgn, c \in (cd \cup cm)$	$(c*r*w)$	$TS_{c,r,w}$	$(c*r*w)$	NO
$TVDEF_{c,r}$	$TV_{c,r} = \left( (tvb_{c,r} + dabtv_{c,r}) * TVADJ_r \right) + (DTV_r * tv01_{c,r})$ $\forall r \in rgn, c \in (cd \cup cm)$	$(c*r*w)$	$TV_{c,r}$	$(c*r)$	NO
$TXDEF_{a,r}$	$TX_{a,r} = \left( (txb_{a,r} + dabtx_{a,r}) * TXADJ_r \right) + (DTX_r * tx01_{a,r})$ $\forall r \in rgn$	$(a*rgn)$	$TX_{a,r}$	$(a*rgn)$	NO
$TYFDEF_{f,r}$	$TYF_{f,r} = \left( (tyfb_{f,r} + dabtyf_{f,r}) * TYFADJ_r \right) + (DTYF_r * tyf01_{f,r})$ $\forall r \in rgn$	$(f*rgn)$	$TYF_{f,r}$	$(f*rgn)$	NO
$TYHDEF_{h,r}$	$TYH_{h,r} = \left( (tyhb_{h,r} + dabtyh_{h,r}) * TYHADJ_r \right) + (DTYH_r * tyh01_{h,r})$ $\forall r \in rgn$	$(h*rgn)$	$TYH_{h,r}$	$(h*rgn)$	NO
$TFDEF_{f,a,r}$	$TF_{f,a,r} = \left( (tfb_{f,a,r} + dabtf_{f,a,r}) * TFADJ_r \right) + (DTF_r * ty01_{f,a,r})$ $\forall r \in rgn$	$(f*a*rgn)$	$TF_{f,a,r}$	$(f*a*rgn)$	NO



Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>GOVERNMENT TAXES BLOCK</b>					
$MTAXEQ_r$	$MTAX_r = \sum_w \sum_c (TM_{w,c,r} * PWM_{w,c,r} * ER_r * QMR_{w,c,r})$ $\forall r \in rgn$	$rgn$	$MTAX_r$	$rgn$	NO
$ETAXEQ_r$	$ETAX_r = \sum_w \sum_c (TE_{c,w,r} * PWE_{c,w,r} * ER_r * QER_{c,w,r})$ $\forall r \in rgn$	$rgn$	$ETAX_r$	$rgn$	NO
$STAXEQ_r$	$STAX_r = \sum_c \left( TS_{c,r} * PQ_{c,r} * (QINTD_{c,r} + QCD_{c,r} + QGD_{c,r} + QINVD_{c,r}) \right)$ $\forall r \in rgn$	$rgn$	$STAX_r$	$rgn$	NO
$VTAXEQ_r$	$VTAX_r = \sum_c \sum_h (TV_{c,r} * PQD_{c,r} * QCD_{c,h,r})$ $\forall r \in rgn$	$rgn$	$INDTAX_r$	$rgn$	NO
$ITAXEQ_r$	$ITAX_r = \sum_a (TX_{a,r} * PX_{a,r} * QX_{a,r})$ $\forall r \in rgn$	$rgn$	$INDTAX_r$	$rgn$	NO
$FYTAXEQ_r$	$FYTAX_r = \sum_f (TYF_{f,r} * (YF_{f,r} - (deprec_{f,r} * YF_{f,r})))$ $\forall r \in rgn$	$rgn$	$FYTAX_r$	$rgn$	NO
$HTAXEQ_r$	$HTAX_r = \sum_h (TYH_{h,r} * YH_{h,r})$ $\forall r \in rgn$	$rgn$	$HTAX_r$	$rgn$	NO
$FTAXEQ_r$	$FTAX_r = \sum_f \sum_a (TF_{f,a,r} * WF_{f,r} * WFDIST_{f,a,r} * FD_{f,a,r})$ $\forall r \in rgn$	$rgn$	$FTAX_r$	$rgn$	NO

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>GOVERNMENT INCOME AND EXPENDITURE BLOCK</b>					
$YGEQ_r$	$YG_r = MTAX_r + ETAX_r + STAX_r + VTAX_r + ITAX_r + FYTAX_r + HTAX_r + FTAX_r \quad \forall r \in rgn$	$rgn$	$YG_r$	$rgn$	NO
$QGDEQ_{c,r}$	$QGD_{c,r} = qgdconst_{c,r} * QGDADJ_r \quad \forall r \in rgn$	$(c*rgn)$	$QGD_{c,r}$	$(c*rgn)$	NO
$EGEQ_r$	$EG_r = \sum_c PQD_{c,r} * QGD_{c,r} \quad \forall r \in rgn$	$rgn$	$EG_r$	$rgn$	NO
<b>KAPITAL ACCOUNT BLOCK</b>					
$SHHDEF_{h,r}$	$SHH_{h,r} = ((shhb_{h,r} + dabshh_{h,r}) * SADJ_r) + (DSHH_r * shh01_{h,r}) \quad \forall r \in rgn$	$rgn$	$SHH_{h,r}$	$rgn$	NO
$TOTSAVEQ_r$	$TOTSAV_r = \left( \sum_h (YH_{h,r} * (1 - TYH_{h,r})) * (SHH_{h,r}) \right) + \sum_f deprec_{f,r} * YF_{f,r} + KAPGOV_r + (KAPWOR_r * ER_r) \quad \forall r \in rgn$	$rgn$	$TOTSAV_r$	$rgn$	NO
$QINVDEQ_{c,r}$	$QINVD_{c,r} = IADJ_r * qinvdconst_{c,r} \quad \forall r \in rgn$	$(c*rgn)$	$QINVD_{c,r}$	$(c*rgn)$	NO
$INVESTEQ_r$	$INVEST_r = \sum_c (PQD_{c,r} * QINVD_{c,r}) \quad \forall r \in rgn$	$rgn$	$INVEST_r$	$rgn$	NO

Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>MARKET CLEARING BLOCK</b>					
$FMEQUIL_{f,r}$	$FS_{f,r} = \sum_a FD_{f,a,r} + UNEMP_{f,r} \quad \forall r \in rgn$	$(f*rgn)$	$FS_{f,r}$	$(f*rgn)$	NO
$UNEMPEQUIL_{f,r}$	$UNEMP_{f,a} \geq 0 \quad \forall r \in rgn$	$(f*rgn)$	$UNEMP_{f,r}$	$(f*rgn)$	NO
$QEQUIL_{c,r}$	$QQ_{c,r} = QINTD_{c,r} + \sum_h QCD_{c,h,r} + QGD_{c,r} + QINVD_{c,r}$ $\forall c \in (cd \cup cm), r \in rgn$	$(c*rgn)$	$QQ_{c,r}$	$(c*rgn)$	NO
$COMTRADE_{c,r}$	$\sum_w (PWM_{w,c,r} * QMR_{w,c,r}) = \sum_w (PWE_{c,w,r} * QER_{c,w,r}) + GLOBESLACK$ $\forall c \in ct2, r \notin rgn$	1	$GLOBESLACK$	1	YES
$TRCONP_{w,c,r}$	$PWMFOB_{w,c,r} = PWE_{c,w,r} \quad \forall c \in cmr, map\_r\_w, map\_w\_r$	$(cmr*r*w)$	$PWMFOB_{c,r,w}$	$(cmr*r*w)$	YES
$TRCONQ_{w,c,r}$	$QMR_{w,c,r} = QER_{c,w,r} \quad \forall c \in cmr, map\_r\_w, map\_w\_r$	$(cmr*r*w)$	$QMR_{c,r,w}$	$(cmr*r*w)$	YES
$GLOBEQUIL_{c,r}$	$\sum_w QT_{w,c,r} = \sum_w QER_{c,w,"glo"} \quad \forall c \in ct2, r \in rgn$	$(ct2*rgn)$		$(ct2*rgn)$	YES
$PTDEF_{c,r}$	$PT_{c,r} = PWE_{c,w,"glo"} \quad \forall c \in ct2, r \in rgn$	$(ct2*rgn)$	$PT_{c,r}$	$(ct,rgn)$	YES
<b>SLACKS BLOCK</b>					
$WALRASEQ_r$	$TOTSAV_r = INVEST_r + WALRAS_r \quad \forall r \in rgn$	$rgn$	$WALRAS_r$	$rgn$	NO
$SYSEQUIL$	$KAPWORSYS = \sum_r KAPWOR_r \quad \forall r \in rgn$	1	$KAPWORSYS$	1	NO



Name	Equation	Number of Equations	Variable	Number of Variables	Globe
<b>MACROECONOMIC CLOSURES BLOCK</b>					
$KAPGOVEQ_r$	$KAPGOV_r = YG_r - EG_r \quad \forall r \in rgn$	$rgn$	$KAPGOV_r$	$rgn$	NO
$KAPREQUIL_{r,w}$	$KAPREG_{w,r} = \left( \sum_c PWMFOB_{w,c,r} * QMR_{w,c,r} \right) - \left( \sum_c PWE_{c,w,r} * QER_{c,w,r} \right)$ $\forall w \in wgn$	$(r*wgn)$	$KAPREG_{r,w}$	$(r*wgn)$	NO
$KAPREQUIL2_{r,w}$	$KAPREG_{w,r} = \left( \sum_c \sum_w PT_{c,r} * QT_{w,c,r} \right) - \left( \sum_c PWE_{c,w,r} * QER_{c,w,r} \right)$ $\forall w \notin wgn$	$r$	$KAPREG_{r,w}$	$r$	YES
$KAPEQUIL_r$	$KAPWOR_r = \sum_w KAPREG_{w,r} \quad \forall r$	$r$	$KAPWOR_r$	$r$	YES
$VFDOMDEQ_r$	$VFDOMD_r = \sum_c \left( PQCD_{c,r} * \sum_h QCD_{c,h,r} \right) + \sum_c \left( PQD_{c,r} * (QGD_{c,r} + QINVD_{c,r}) \right)$ $\forall r \in rgn$	$rgn$	$VFDOMD_r$	$rgn$	NO
$INVESTSHEQ_r$	$INVESTSH_r * VFDOMD_r = INVEST_r \quad \forall r \in rgn$	$rgn$	$INVESTSH_r$	$rgn$	NO
$VGDSHEQ_r$	$INVESTSH_r * VFDOMD_r = INVEST_r \quad \forall r \in rgn$	$rgn$	$VGDSH_r$	$rgn$	NO



ANARRES\_t: A SAM Based Global CGE Model.....

Name	Equation	Number of Equations	Variable	Number of Variables
<b>MODEL CLOSURE</b>				
	All globe transactions are in world dollars (i.e. of the reference region)	$\overline{ER}_{glo}$		
	There is no current account equation for the globe.	AND $\overline{KAPWOR}_{glo}$		
	Assign the reference region, eliminating one variable; add the constraint that the sum of KAPWOR across <i>rgn</i> must be zero	$\overline{KAPWORSYS}$	$\overline{ER}_{ref}$	
	For the non-reference regions, one can fix either the exchange rate or the current account balance	$\overline{ER}_{nonref}$ or $\overline{KAPWOR}_{nonref}$		1
		$\overline{SADJ}$ or $\overline{IADJ}$ or $\overline{INVEST}$		1
	All <b>but</b> two of $\overline{TMADJ}, \overline{TMSADJ}, \overline{TSADJ}, \overline{TVADJ}, \overline{TEADJ}, \overline{TXADJ}, \overline{TYHADJ}, \overline{QGDADJ}, \overline{KAPGOV}, \overline{EG}$			6
			$\overline{FS}_f$	3
			$\overline{CPI}$ or $\overline{PPI}$	1
		$f + 12c + (4+f)a + 14$	$2f + 12c + (4+f)a + 23$	



## References

- de Melo, J. and Robinson, S., (1989). 'Product Differentiation and the Treatment of Foreign Trade in Computable General Equilibrium Models of Small Economies', *Journal of International Economics*, Vol 27, pp 47-67.
- Devarajan, S., Lewis, J.D. and Robinson, S., (1990). 'Policy Lessons from Trade-Focused, Two-Sector Models', *Journal of Policy Modeling*, Vol 12, pp 625-657.
- Drud, A., Grais, W. and Pyatt, G., (1986). 'Macroeconomic Modelling Based on Social-Accounting Principles', *Journal of Policy Modeling*, Vol 8, pp 111-145.
- Hertel, T.W., (1997). *Global Trade Analysis: Modeling and Applications*. Cambridge: Cambridge University Press.
- Kilkenny, M., (1991). Computable General Equilibrium Modelling of Agricultural Policies: Documentation of the 30-Sector FPGE GAMS Model of the United States. *USDA ERS Staff Report AGES 9125*.
- Kilkenny, M. and Robinson, S., (1990). 'Computable General Equilibrium Analysis of Agricultural Liberalisation: Factor Mobility and Macro Closure', *Journal of Policy Modeling*, Vol 12, pp 527-556.
- Lewis, J., Robinson, S., and Wang, Z. (
- Löfgren, H., Harris, R.L. and Robinson, S., with Thomas, M. and El-Said, M., (2002). *Microcomputers in Policy Research 5: A Standard Computable General Equilibrium (CGE) Model in GAMS*. Washington: IFPRI.
- McDonald, S. and Sonmez, Y., (2004). 'Augmenting the GTAP Database with Data on Inter-Regional Transactions', *Sheffield Economics Research Paper 2004:009*. The University of Sheffield
- McDonald, S., (2003). 'A Standard Computable General Equilibrium Model: Technical Documentation', *PROVIDE Project Technical Paper 2003:03*. Elsenburg, RSA.
- McDonald, S. and Thhalefang, J., (2001). 'CGE Models of Energy Use: A Review of Production Structures and Data Requirements', *Report for the RANESA Project 'Energy Accounts for Botswana'*.
- McDonald, S., and Thierfelder, K., (2004a). 'Deriving a Global Social Accounting Matrix from GTAP version 5 Data', *GTAP Technical Paper 23*. Global Trade Analysis Project: Purdue University.
- McDonald, S., and Thierfelder, K., (2004b). 'Deriving Reduced Form Global Social Accounting Matrices from GTAP Data', *mimeo*.
- McDonad, S. and Thierfelder, K., (2019). 'Deriving a Global Social Accounting Matrix and Satellite Data from GTAP Databases', *CGEMOD Technical Paper 12*.

(<http://www.cgemod.org.uk/Deriving%20a%20Global%20GTAP%20SAM%20cgemod%20TP%2012.pdf>)

- McDonald, S. and Sonmez, Y., (2006), 'Labour Migration and Remittances: Some Implications of Turkish "Guest Workers" in Germany', *9th Annual Conference on Global Economic Analysis*, UN Economic Commission for Africa, Addis Ababa, Ethiopia, June.
- McDonald, S., and Thierfelder, K., (2006). 'The Doha Development Agenda and Africa: Taking Armington Seriously', *9th Annual Conference on Global Economic Analysis*, UN Economic Commission for Africa, Addis Ababa, Ethiopia, June.
- PROVIDE (2004a). 'SeeResults: A Spreadsheet Application for the Analysis of CGE Model Results', *PROVIDE Technical Paper*, 2004:1. Elsenburg, RSA.
- PROVIDE (2004b). 'SAMGator: A Spreadsheet Application for the Aggregation of Social Accounting Matrices', *PROVIDE Technical Paper*, forthcoming. Elsenburg, RSA.
- Pyatt, G., (1987). 'A SAM Approach to Modelling', *Journal of Policy Modeling*, Vol 10, pp 327-352.
- Pyatt, G., (1991). 'Fundamentals of Social Accounting', *Economic Systems Research*, Vol 3, pp 315-341.
- Robinson, S., (2004). 'Exchange Rates in Global CGE Models', paper presented at the *IIOA and EcoMod Conference*, Brussels, Sept 2004.
- Robinson, S., Burfisher, M.E., Hinojosa-Ojeda, R. and Thierfelder, K.E., (1993). 'Agricultural Policies and Migration in a US-Mexico Free Trade Area: A Computable General Equilibrium Analysis', *Journal of Policy Modeling*, Vol 15, pp 673-701.
- Robinson, S., Kilkenny, M. and Hanson, K., (1990). 'USDA/ERS Computable General Equilibrium Model of the United States', Economic Research Services, USDA, *Staff Report AGES 9049*.
- Sen, A.K., (1963). 'Neo-classical and Neo-Keynesian Theories of Distribution', *Economic Record*, Vol 39, pp 53-64.
- Stone, R., (1962a). 'A Computable Model of Economic Growth', *A Programme for Growth: Volume 1*. Cambridge: Chapman and Hall.
- Stone, R., (1962b). 'A Social Accounting Matrix for 1960', *A Programme for Growth: Volume 2*. Cambridge: Chapman and Hall.
- Tlhalefang, J., (2006). *Computable General Equilibrium Implications of Oil Shocks and Policy Responses in Botswana*, unpublished PhD thesis, Department of Economics, University of Sheffield.
- UN, (1993). *System of National Accounts 1993*. New York: UN.